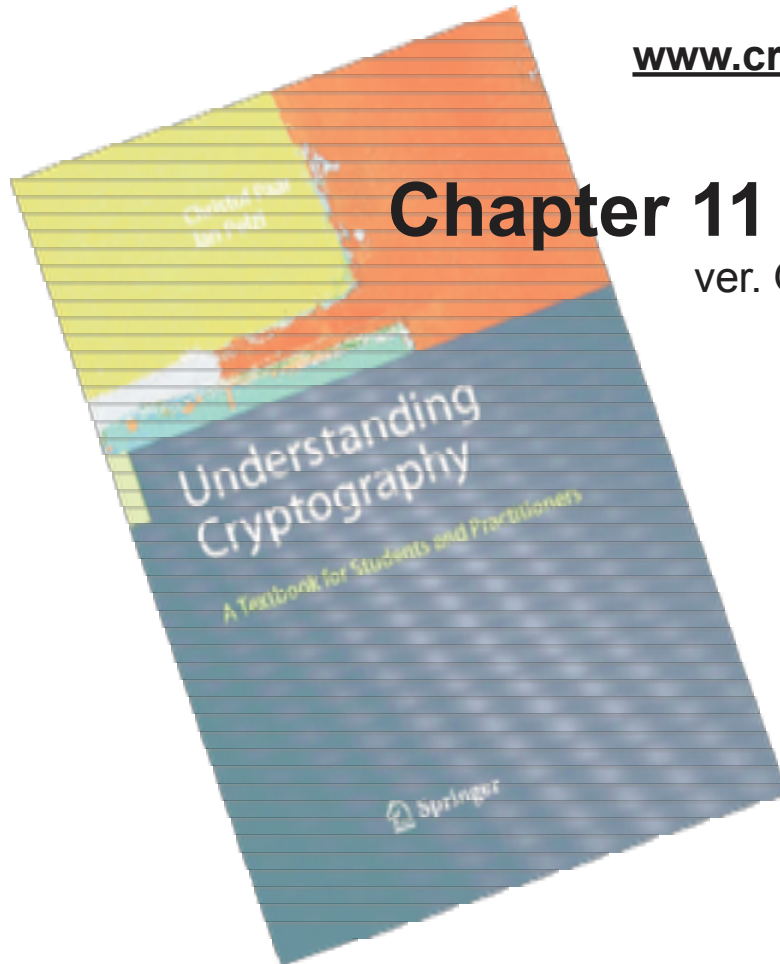


# Understanding Cryptography – A Textbook for Students and Practitioners

by Christof Paar and Jan Pelzl

[www.crypto-textbook.com](http://www.crypto-textbook.com)



## Chapter 11 – Hash Functions

ver. October 29, 2009

These slides were prepared by Stefan Heyse and Christof Paar and Jan Pelzl  
And modified by Sam Bowne

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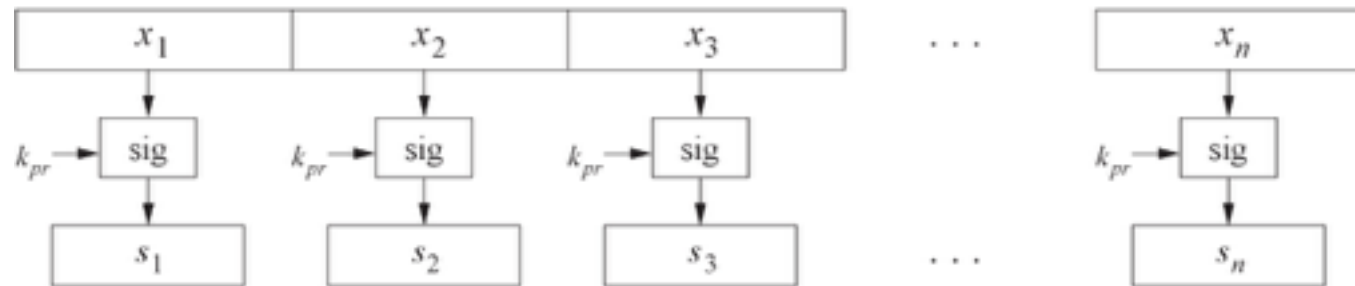
11.4 The Secure Hash Algorithm SHA-1

# 11.1 Motivation: Signing Long Messages

# Motivation

## Problem:

Naive signing of long messages generates a signature of same length.



- Three Problems
- Computational overhead
- Message overhead
- Security limitations
  - Attacker could re-order or re-use signed blocks

## Solution:

Instead of signing the whole message, sign only a digest (=hash)

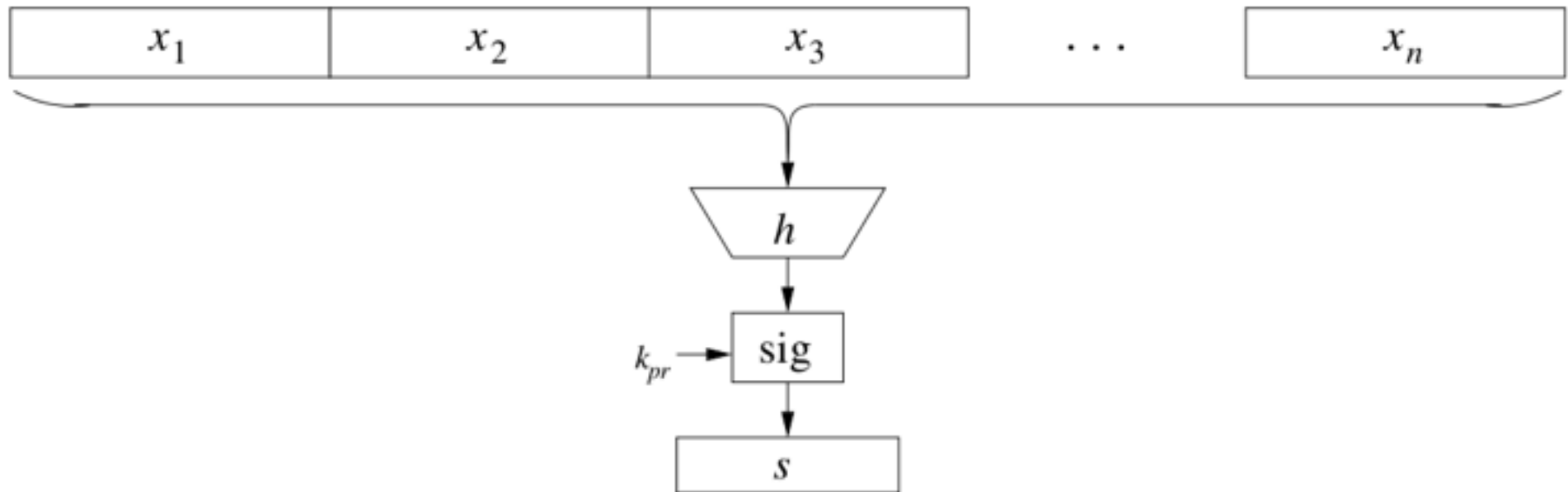
Also secure, but much faster

## Needed:

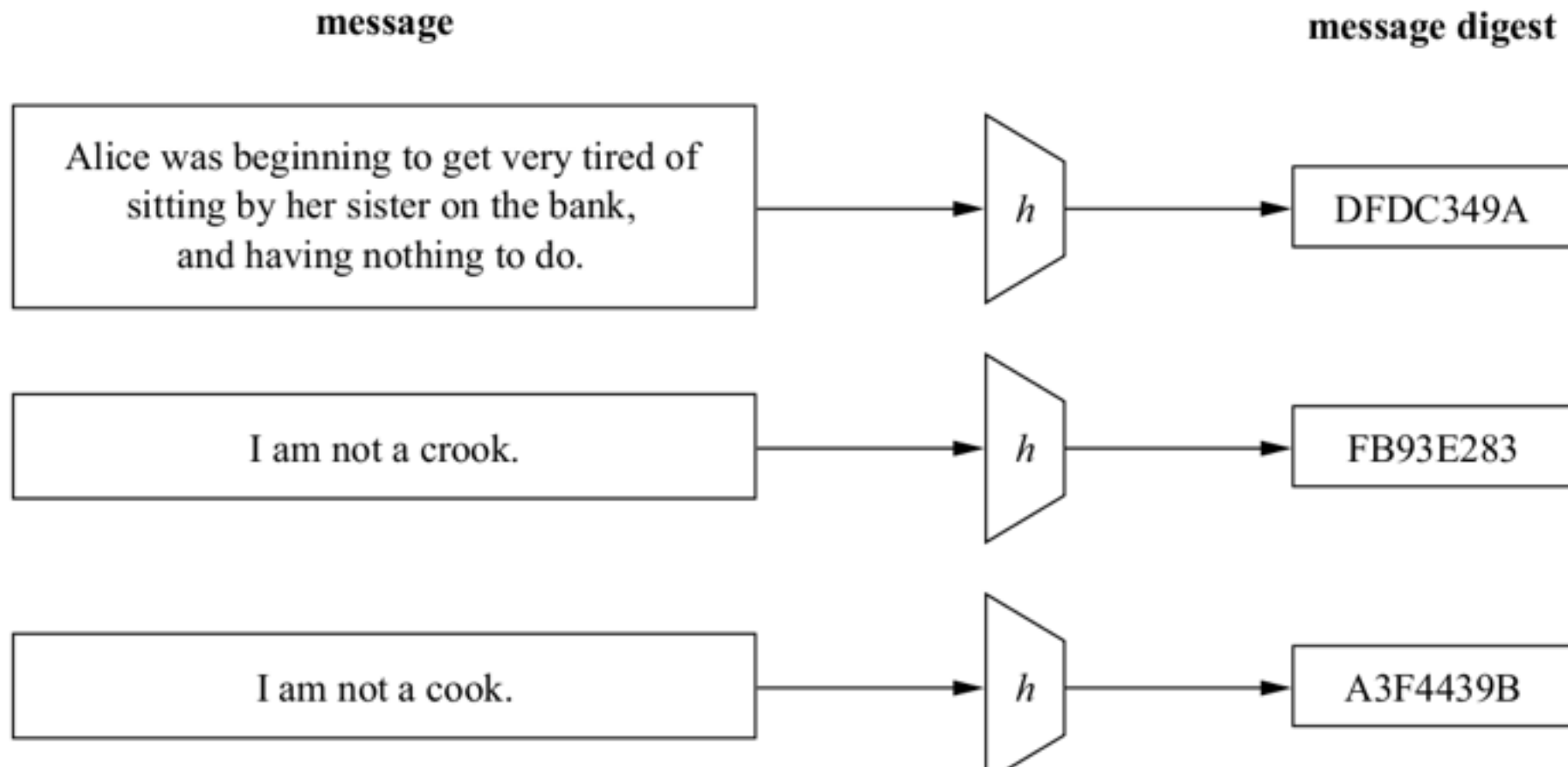
5 Hash Functions

# Solution

- Hash, then sign



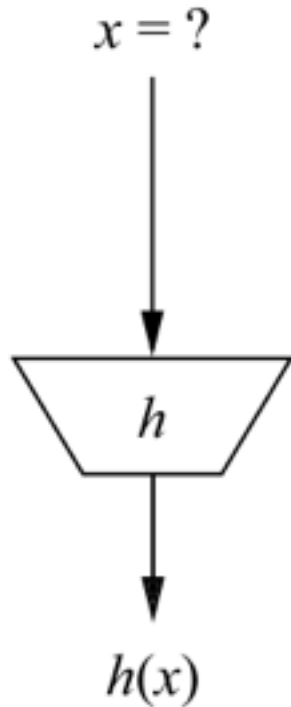
# Principal input–output behavior of hash functions



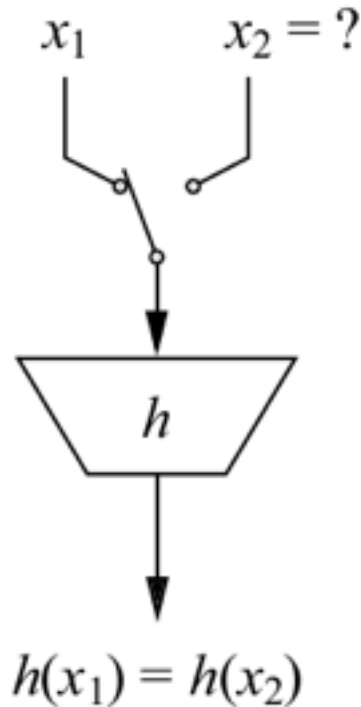
## 11.2 Security Requirements of Hash Functions



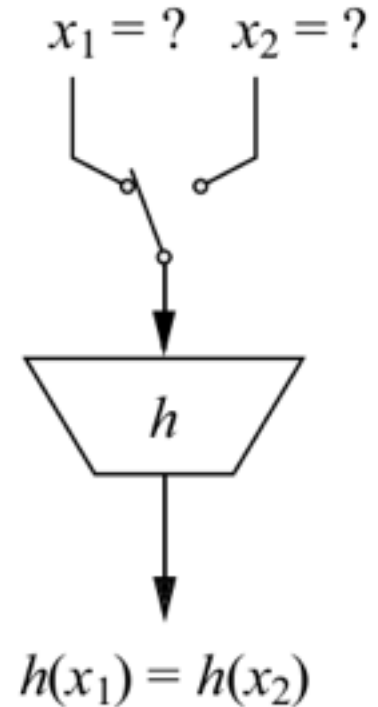
# The three security properties of hash functions



preimage resistance



second preimage



collision resistance

# Hash Functions: Security Properties

- **Preimage resistance:** For a given output  $z$ , it is impossible to find any input  $x$  such that  $h(x) = z$ , i.e.,  $h(x)$  is one-way  
(Also called **one-wayness**)
- **Second preimage resistance:** Given  $x_1$ , and thus  $h(x_1)$ , it is computationally infeasible to find any  $x_2$  such that  $h(x_1) = h(x_2)$   
(Also called **weak collision resistance**)
- **Collision resistance:** It is computationally infeasible to find any pairs  $x_1 \neq x_2$  such that  $h(x_1) = h(x_2)$   
(Also called **strong collision resistance**)

# Hash Functions: Security

- Collision resistance causes most problems
- How hard is it to find a collision with a probability of 0.5 ?
- Related Problem: How many people are needed such that two of them have the same birthday with a probability of 0.5 ?
- No! Not  $365/2=183$
- 23 are enough ! This is called the birthday paradox (Search takes  $\approx\sqrt{2n}$  steps)
- To deal with this paradox, hash functions need a output size of at least 160 bits

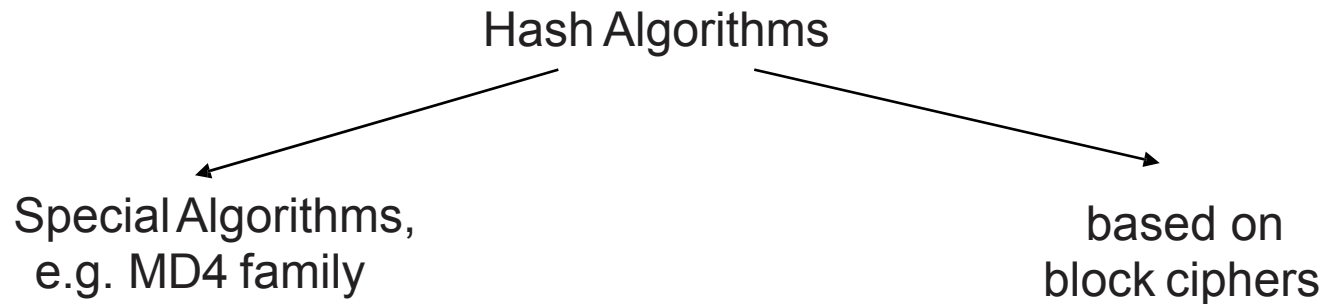
# Hash Functions: Security

**Table 11.1** Number of hash values needed for a collision for different hash function output lengths and for two different collision likelihoods

$\lambda$	Hash output length				
	128 bit	160 bit	256 bit	384 bit	512 bit
0.5	$2^{65}$	$2^{81}$	$2^{129}$	$2^{193}$	$2^{257}$
0.9	$2^{67}$	$2^{82}$	$2^{130}$	$2^{194}$	$2^{258}$

## 11.3 Overview of Hash Algorithms

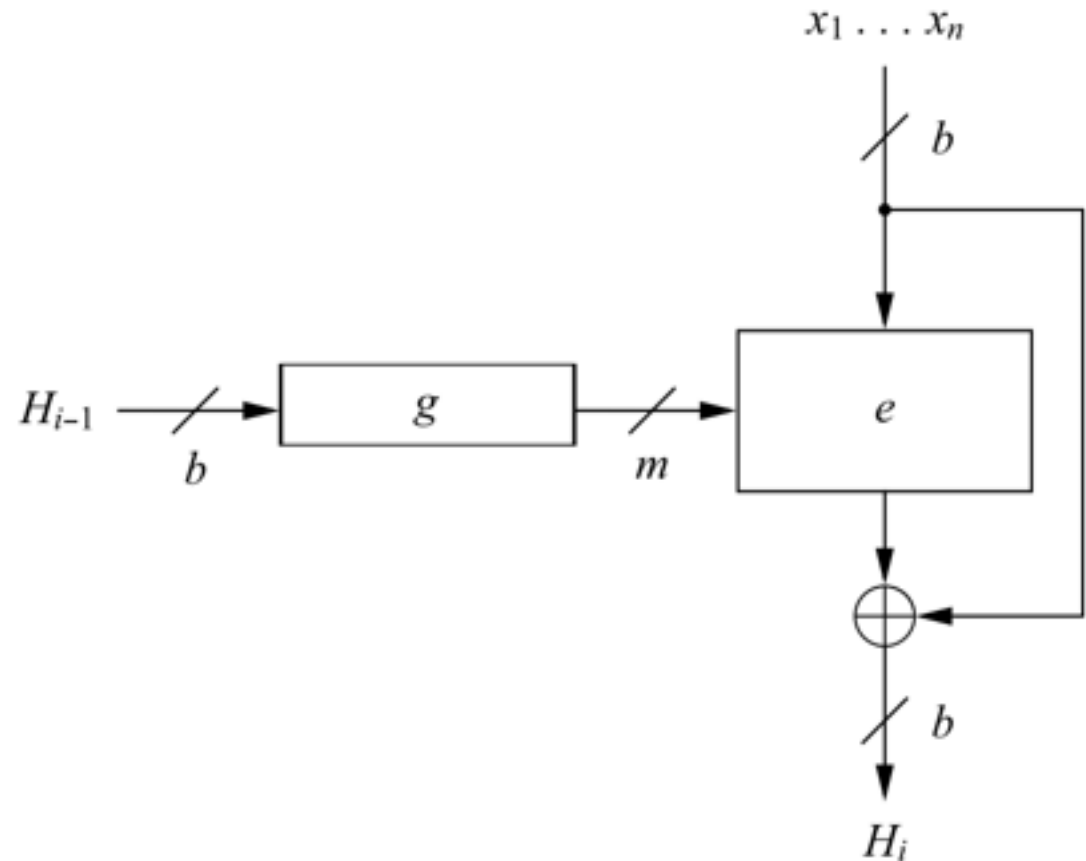
# Hash Functions: Algorithms



- **MD4** family
- **SHA-1**: output - 160 Bit; input - 512 bit chunks of message  $x$ ; operations - bitwise AND, OR, XOR, complement and cyclic shifts.
- **RIPE-MD 160**: output - 160 Bit; input - 512 bit chunks of message  $x$ ; operations – like in SHA-1, but two in parallel and combinations of them after each round.

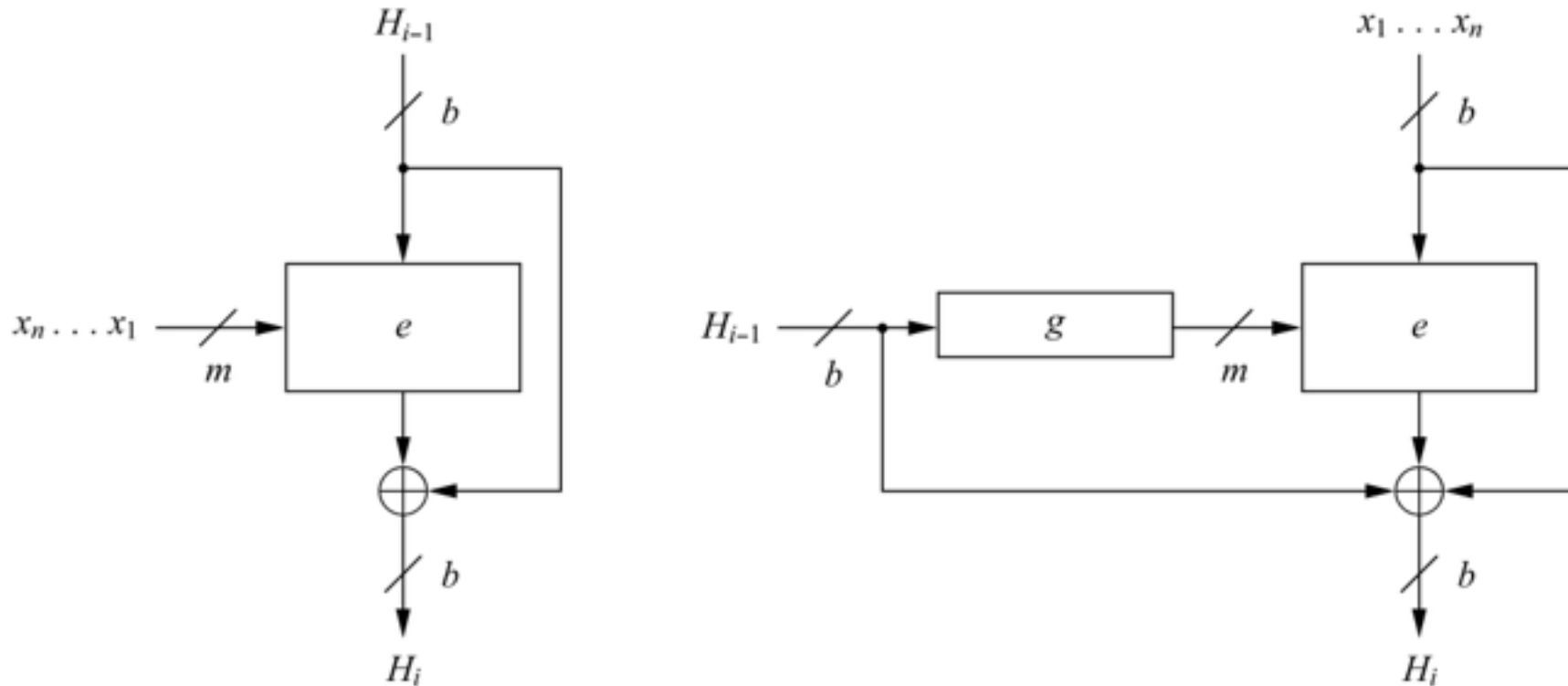
# Hash Functions from Block Ciphers

- Matyas-Meyer-Oseas hash function
- Break original file into blocks
- Start with known public block  $H_0$ , which may be all zeroes
- Encrypt a block using previous  $H$  as the key, then XOR with next block of file data to form the new  $H$
- Repeat through whole file



$$H_i = e_{g(H_{i-1})}(x_i) \oplus x_i$$

# Other Hash Functions from Block Ciphers



$$H_i = H_{i-1} \oplus e_{x_i}(H_{i-1})$$

(Davies–Meyer)

$$H_i = H_{i-1} \oplus x_i \oplus e_{g(H_{i-1})}(x_i)$$

(Miyaguchi–Preneel)



## 11.4 The Secure Hash Algorithm SHA-1

# SHA-1

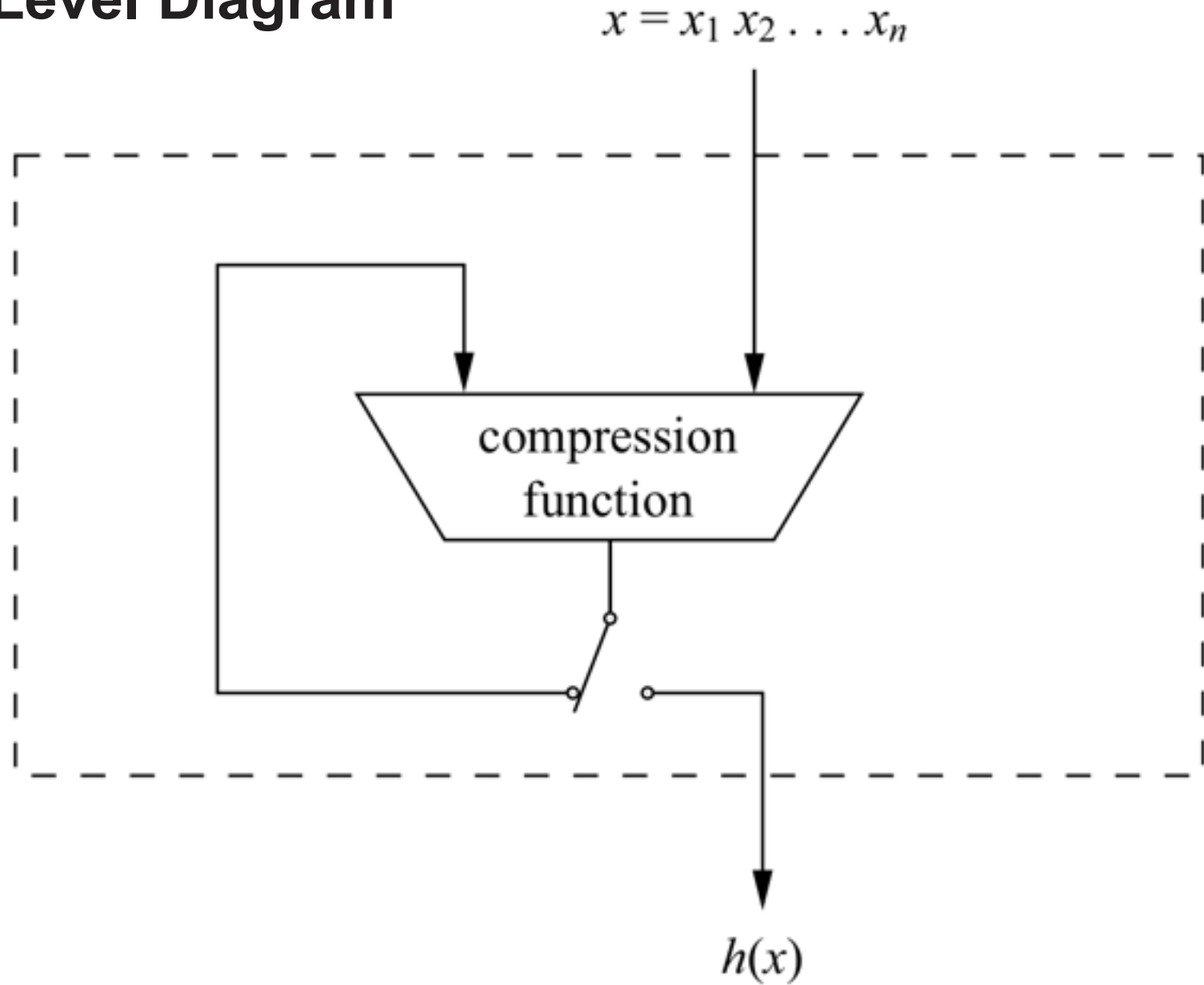
- Part of the MD-4 family.
- Based on a Merkle-Damgård construction
- Similar to a Feistel block cipher
- 160-bit output from a message of maximum length  $2^{64}$  bit.
- Widely used ( even tough some weaknesses are known)

# How Big is $2^{60}$ bits?

- $2^{10} = 1024 = 1\text{Kb}$
- $2^{20} = 1\text{Mb}$
- $2^{30} = 1\text{Gb}$
- $2^{40} = 1\text{ Tb}$
- $2^{60} = 1\text{ million Tb}$
- $2^{63} = 1\text{ million TB}$
- $2^{54} = 2\text{ million TB}$

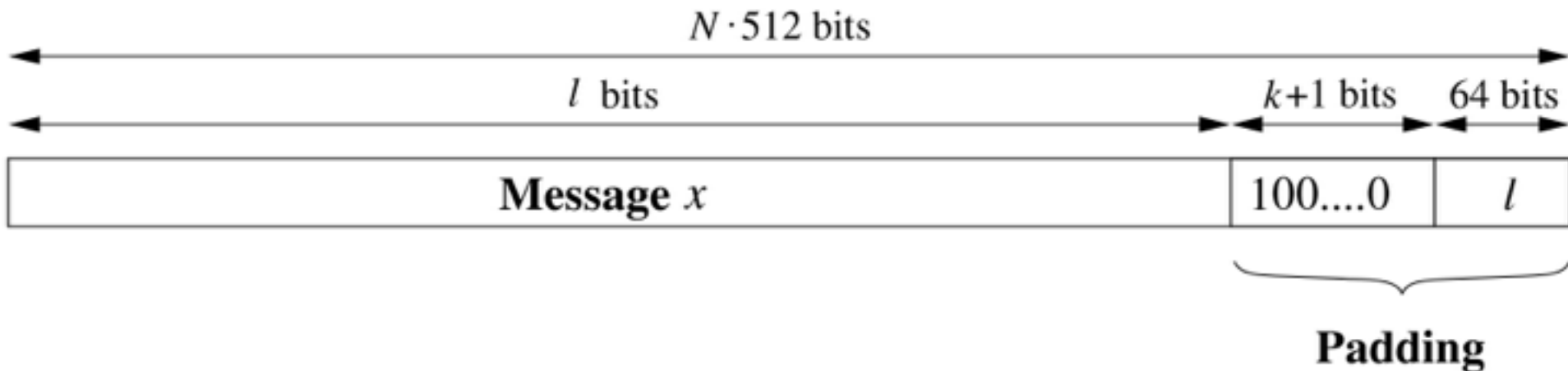
# SHA-1 High Level Diagram

Compression Function consists of 80 rounds which are divided into four stages of 20 rounds each



# SHA-1: Padding

- Message  $x$  has to be padded to fit a size of a multiple of 512 bits
- Add  $k$  zero bits
- $k = 512 - 64 - 1 - l = 448 - (l + 1) \bmod 512$



# SHA-1: Padding Example

- Message is **abc**  
24 bits long

01100001  
a

01100010  
b

01100011  
c

$$k = 512 - 64 - 1 - 24 = 423$$

01100001  
a

01100010  
b

01100011  
c

1

00...0  
423 zeros

00...011000  
64 bits long  
Value = 24 in binary

# SHA-1: Hash Computation

- Each message block  $x_i$  is processed in four stages with 20 rounds each

## SHA-1 uses:

- A message schedule which computes a 32-bit word  $W_0, W_1, \dots, W_{79}$  for each of the 80 rounds
- Five working registers of size of 32 bits  $A, B, C, D, E$
- A hash value  $H_i$  consisting of five 32-bit words  $H_i^{(0)}, H_i^{(1)}, H_i^{(2)}, H_i^{(3)}, H_i^{(4)}$
- In the beginning, the hash value holds the initial value  $H_0$ , which is replaced by a new hash value after the processing of each single message block.
- The final hash value  $H_n$  is equal to the output  $h(x)$  of SHA-1.

**Initial value  $H_0$**  A 160-bit buffer is used to hold the initial hash value for the first iteration. The five 32-bit words are fixed and given in hexadecimal notation as:

$$A = H_0^{(0)} = 67452301$$

$$B = H_0^{(1)} = \text{EFCDAB89}$$

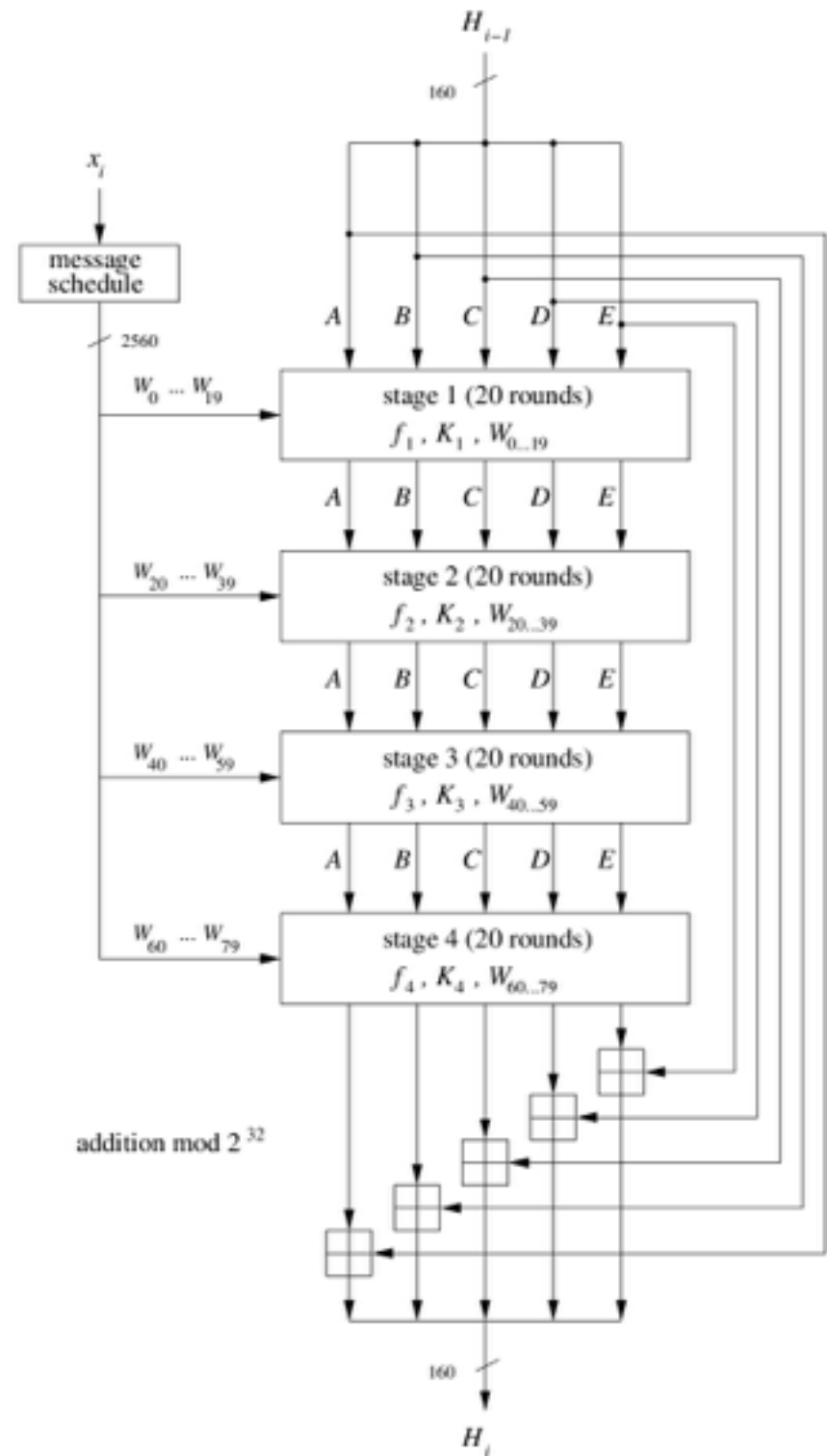
$$C = H_0^{(2)} = 98BADCFE$$

$$D = H_0^{(3)} = 10325476$$

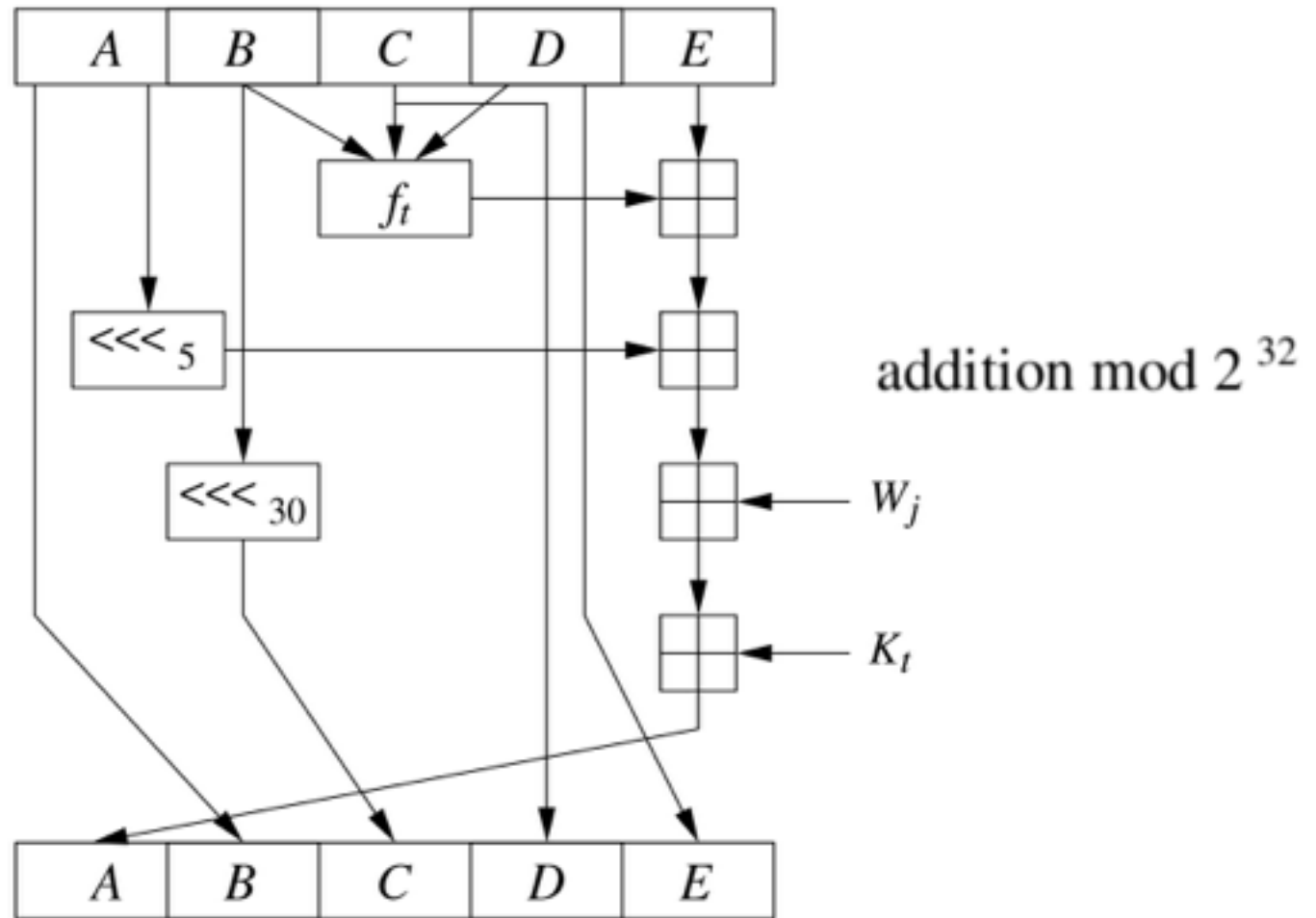
$$E = H_0^{(4)} = \text{C3D2E1F0}.$$



# SHA-1: All four stages



# SHA-1: Internals of a Round



Stage $t$	Round $j$	Constant $K_t$	Function $f_t$
1	00...19	5A827999	$(B \wedge C) \vee (\bar{B} \wedge D)$
2	20...39	6ED9EBA1	$B \oplus C \oplus D$
3	40...59	8F1BBCDC	$(B \oplus C) \vee (B \oplus D) \vee (C \oplus D)$
4	60...79	CA62C1D6	$B \oplus C \oplus D$

AND  $\wedge$   
 OR  $\vee$   
 NOT  $\bar{\phantom{x}}$   
 XOR  $\oplus$

# SHA-1 Collision Found

- Collision found on Feb. 23, 2017
  - Links Ch 12-2017-1, 2, and 3 in CNIT 123

```
[Sams-MacBook-Pro-3:proj14 sambowne$ ls -l sha*  
-rw-r--r--@ 1 sambowne  staff  422435 Feb 23  2017 shattered-1.pdf  
-rw-r--r--@ 1 sambowne  staff  422435 Feb 23  2017 shattered-2.pdf  
[Sams-MacBook-Pro-3:proj14 sambowne$ shasum shattered-1.pdf  
38762cf7f55934b34d179ae6a4c80cadccb7f0a  shattered-1.pdf  
[Sams-MacBook-Pro-3:proj14 sambowne$ shasum shattered-2.pdf  
38762cf7f55934b34d179ae6a4c80cadccb7f0a  shattered-2.pdf  
[Sams-MacBook-Pro-3:proj14 sambowne$ md5 shattered-1.pdf  
MD5 (shattered-1.pdf) = ee4aa52b139d925f8d8884402b0a750c  
[Sams-MacBook-Pro-3:proj14 sambowne$ md5 shattered-2.pdf  
MD5 (shattered-2.pdf) = 5bd9d8cab46041579a311230539b8d1
```

# Google Security Blog

The latest news and insights from Google on security and safety on the Internet

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## Announcing the first SHA1 collision

February 23, 2017

**'First ever' SHA-1 hash collision calculated. All it took were five clever brains... and 6,610 years of processor time**

# SHATTERED

## Collision attack: same hashes



Good doc



Sha-1



3713..42



Bad doc



Sha-1



3713..42

# Browsers Deprecated SHA-1

*Microsoft, Google, and Mozilla will begin phasing out trust for SHA-1 certificates in 2016. With these dates approaching, it's time to move to SHA-2.*

- November 2014 –** *SHA-1 SSL Certificates expiring any time in 2017 will show a warning in Chrome.*
- December 2014 –** *SHA-1 SSL Certificates expiring after June 1, 2016, will show a warning in Chrome.*
- January 2015 –** *SHA-1 SSL Certificates expiring any time in 2016 will show a warning in Chrome.*
- December 2015 –** *SHA-1 SSL Certificates issued after January 1, 2016, will show the "untrusted connection" error in Firefox.*
- January 2016 –** *SHA-1 SSL Certificates issued after January 1, 2016, will show a certificate error in Chrome.  
Certificate criteria: signed with a SHA-1-base signature, issued after January 1, 2016, and chained to a public CA.*
- January 1, 2017 –** *Microsoft, Google, and Mozilla will end trust for all SHA-1 SSL Certificates.  
Mozilla and Google say it is feasible to move this date up to July 1, 2016, in light of recent attacks on SHA-1.  
Microsoft says it is feasible to move this date up to as early as June 2016, in light of recent attacks on SHA-1.*

- Link Ch 12zr in CNIT 123

## ■ Lessons Learned: **Hash-Functions**

- Hash functions are keyless. The two most important applications of hash functions are their use in digital signatures and in message authentication codes such as HMAC.
- The three security requirements for hash functions are one-wayness, second preimage resistance and collision resistance.
- Hash functions should have at least 160-bit output length in order to withstand collision attacks; 256 bit or more is desirable for long-term security.
- MD5, which was widely used, is insecure. Serious security weaknesses have been found in SHA-1, and the hash function should be phased out. The SHA-2 algorithms all appear to be secure.
- The ongoing SHA-3 competition will result in new standardized hash functions in a few years.

**Kahoot!**