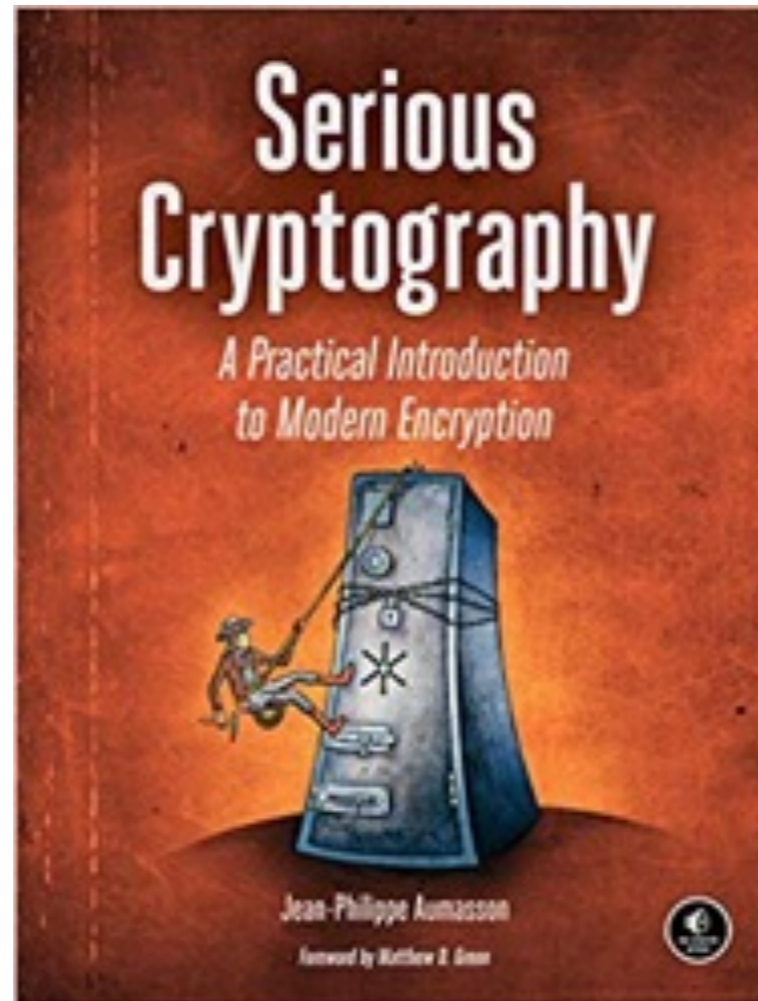


# CNIT 141

## Cryptography for Computer Networks



### 4. Block Ciphers

Updated 9-18-23

# Topics

- What is a Block Cipher
- How to Construct Block Ciphers
- The Advanced Encryption Standard (AES)
- Implementing AES
- Modes of Operation
- How Things Can Go Wrong

# History

- US: Federal standard: DES (1979 - 2005)
- KGB: GOST 28147-89 (1990 - present)
- in 2000, NIST selected AES, developed in Belgium
- They are all *block ciphers*

# What is a Block Cipher

# Block Cipher

**E** Encryption algorithm

**K** Key

**P** Plaintext block

**C** Ciphertext block

$$C = E(K, P)$$

**D** Decryption algorithm

$$P = D(K, C)$$

# Security Goals

- Block cipher should be a *pseudorandom permutation (PRP)*
  - Attacker can't compute output without the key
- Attackers should be unable to find *patterns* in the inputs/output values
- The ciphertext should appear random

# Block Size

- DES: 64 bit
- AES: 128 bit
- Chosen to fit into registers of CPUs for speed
- Block sizes below 64 are vulnerable to a *codebook attack*

# Codebook Attack

- Suppose you can encrypt arbitrary plaintext, such as in a Wi-Fi network, but you don't know the key
  - Encrypt every possible plaintext, place in a *codebook*
  - Look up blocks of ciphertext in the *codebook*



# Codebook Attack

- The codebook size depends on the block size
- Blocksize of 32 bits requires  $2^{32}$  entries
  - 4 billion, easily achieved
- Blocksize of 64 bits requires  $2^{64}$  entries
  - Impossible to achieve
- So blocksize should be 64 or larger

# How to Construct Block Ciphers

# Two Techniques

- Substitution-permutation (AES)
- Feistel (DES)

# Rounds

- **R** is a *round* --in practice, a simple transformation
- A block cipher with three rounds:
  - $C = R_3(R_2(R_1(P)))$
- **iR** is the inverse round function
  - $P = iR_1(iR_2(iR_3(C)))$

# Round Key

- The round functions  $R_1 R_2 R_3$  use the same algorithm
- But a different *round key*
- Round keys are  $K_1, K_2, K_3, \dots$  derived from the main key  $K$  using a *key schedule*

# The Slide Attack and Round Keys

- Consider a block cipher with three rounds, and with all the round keys identical

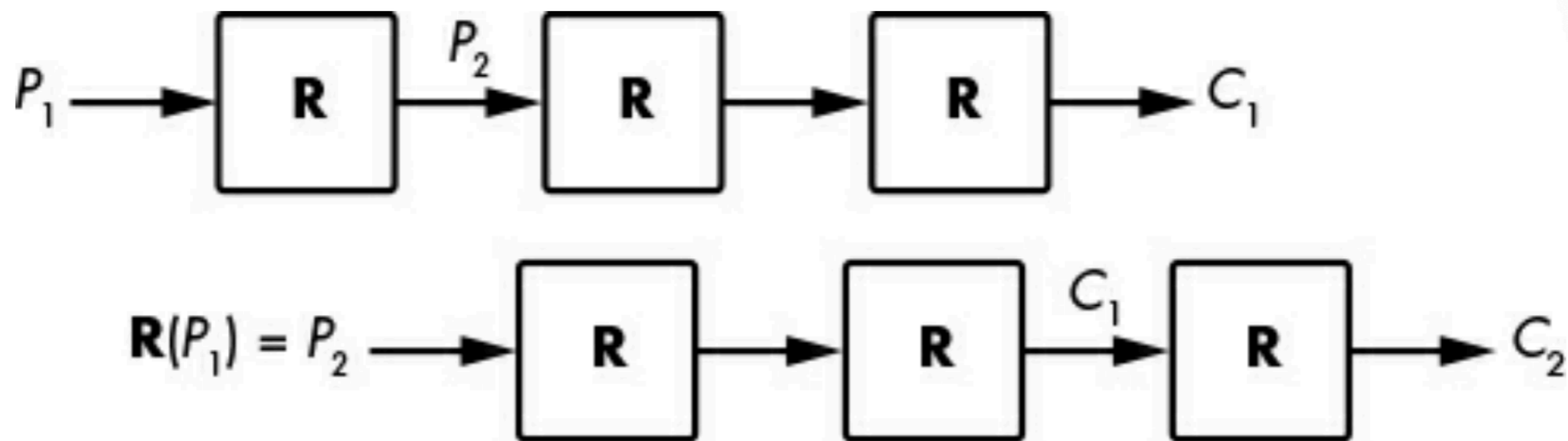


Figure 4-1: The principle of the slide attack, against block ciphers with identical rounds

# The Slide Attack and Round Keys

- If an attacker can find plaintext blocks with  $P_2 = \mathbf{R}(P_1)$
- That implies  $C_2 = \mathbf{R}(C_1)$
- Which often helps to deduce the key

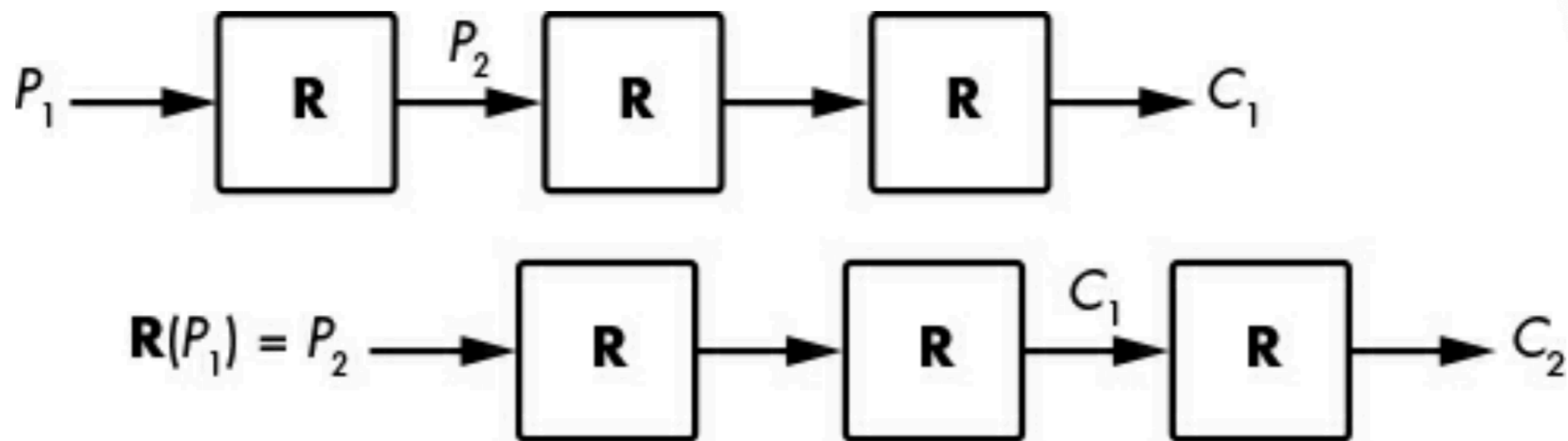


Figure 4-1: The principle of the slide attack, against block ciphers with identical rounds

# The Slide Attack and Round Keys

- The solution is to make all round keys different
- Note: the key schedule in AES is not one-way
  - Attacker can compute  $\mathbf{K}$  from any  $\mathbf{K}_i$
  - This exposes it to side-channel attacks, like measuring electromagnetic emanations

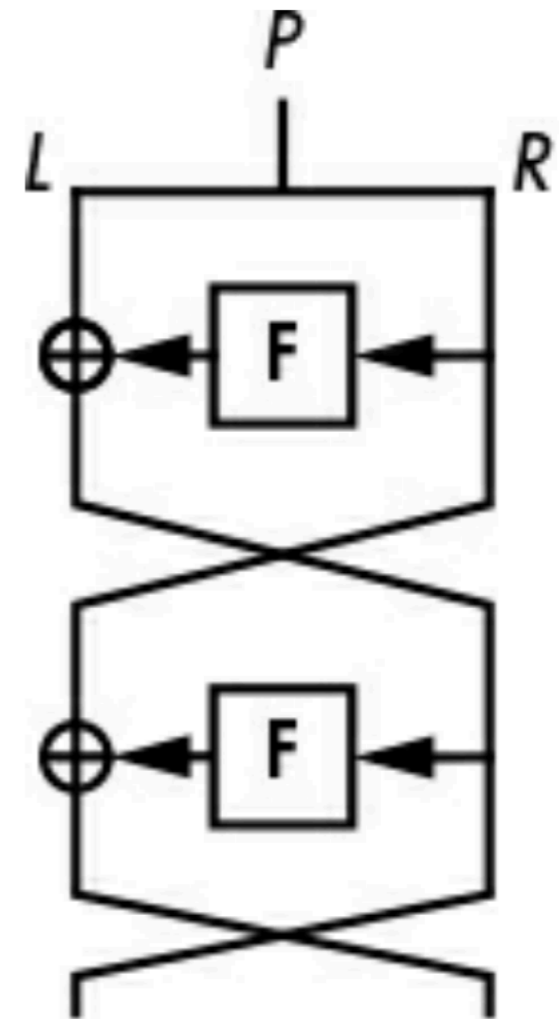


# Substitution-Permutation Networks

- ***Confusion*** means that each ciphertext bit depends on several key bits
  - Provided by ***substitution*** using ***S-boxes***
- ***Diffusion*** means that changing a bit of plaintext changes many bits in the ciphertext
  - Provided by ***permutation***

# Feistel Schemes

- Only half the plaintext is encrypted in each round
  - By the **F** substitution-permutation function
- Halves are swapped in each round
- DES uses 16 Feistel rounds



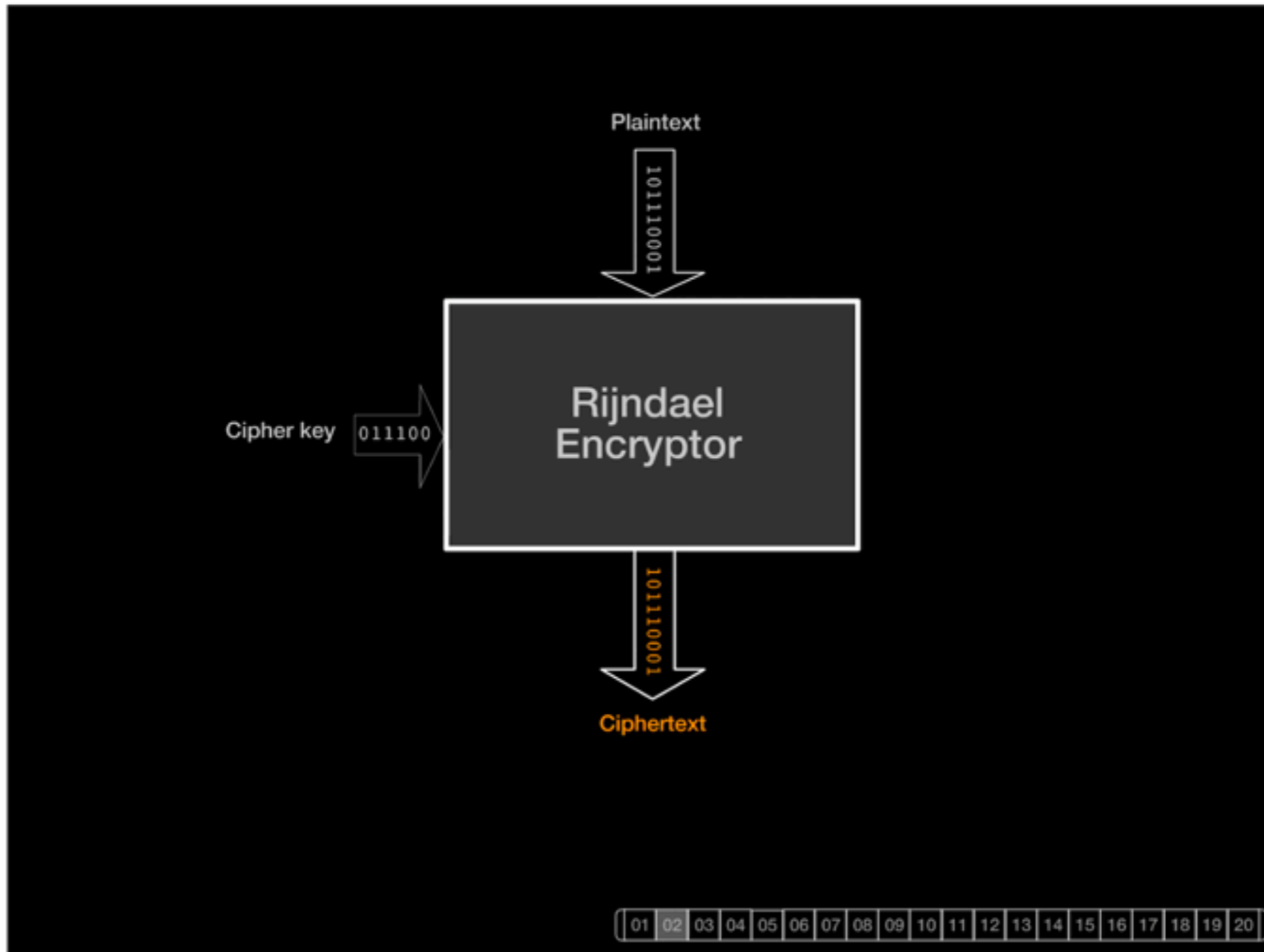


4a

# The Advanced Encryption Standard (AES)

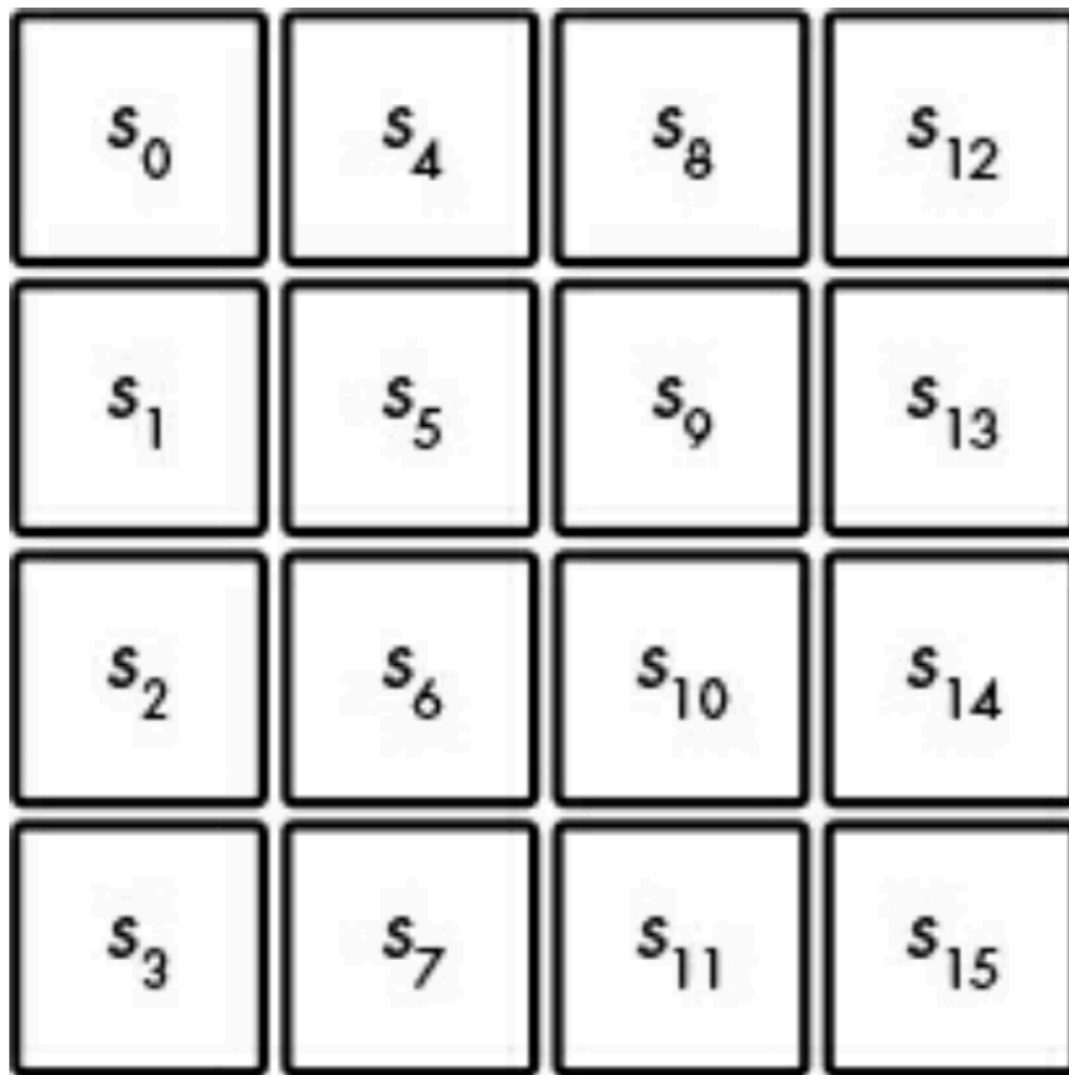
# DES

- DES had a 56-bit key
  - Cracked by brute force in 1997
- 3DES was a stronger version
  - Still considered strong, but slower than AES
- AES approved as the NIST standard in 2000

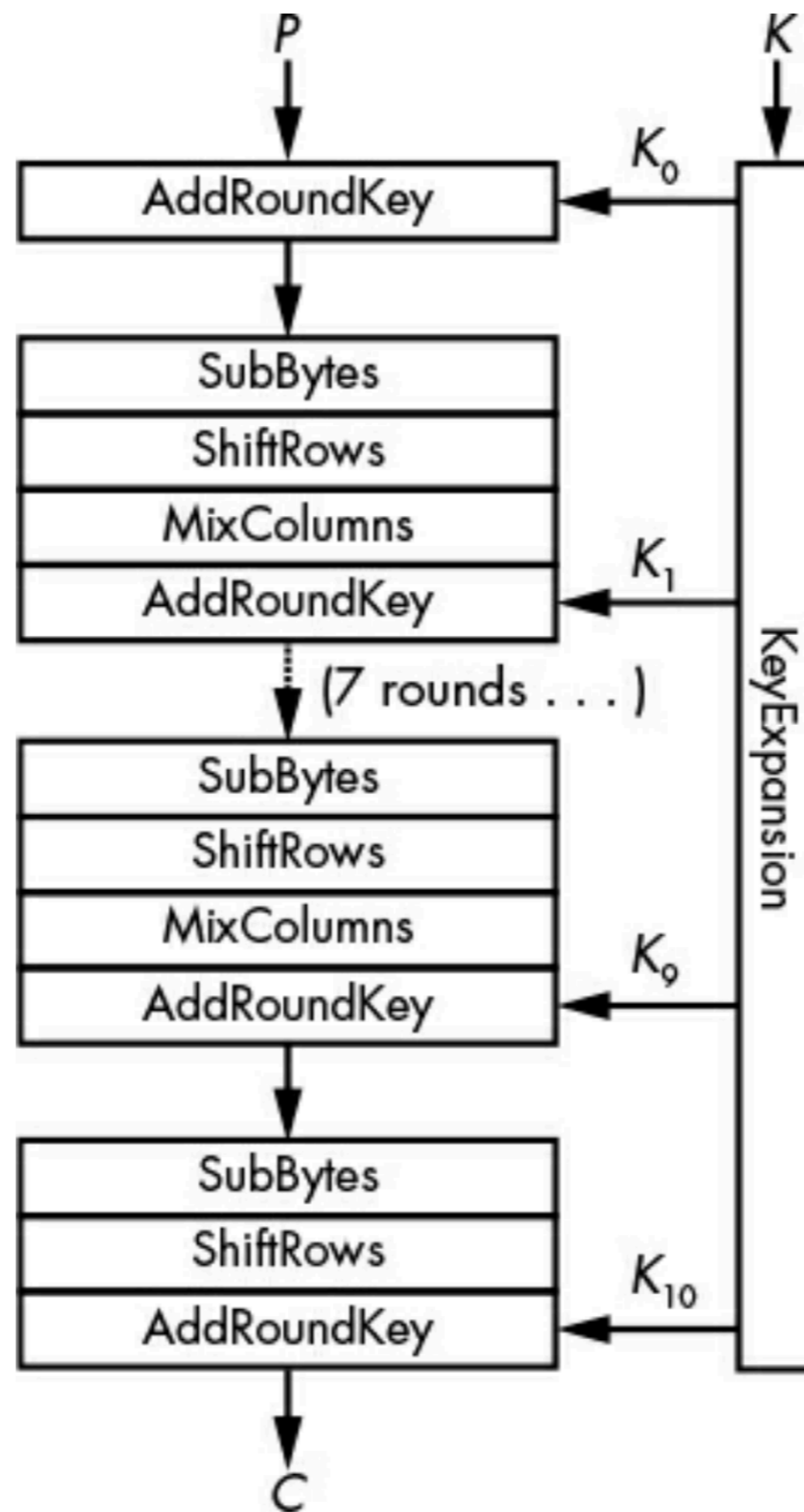


AES Rijndael Cipher explained as a Flash animation

- [Link Ch 4a](#)



*Figure 4-3: The internal state of AES viewed as a  $4 \times 4$  array of 16 bytes*





- **Without KeyExpansion, all rounds would use the same key,  $K$ , and AES would be vulnerable to slide attacks.**
- **Without AddRoundKey, encryption wouldn't depend on the key; hence, anyone could decrypt any ciphertext without the key.**
- **SubBytes brings nonlinear operations, which add cryptographic strength. Without it, AES would just be a large system of linear equations that is solvable using high-school algebra.**
- **Without ShiftRows, changes in a given column would never affect the other columns, meaning you could break AES by building four  $2^{32}$ -element codebooks for each column. (Remember that in a secure block cipher, flipping a bit in the input should affect all the output bits.)**
- **Without MixColumns, changes in a byte would not affect any other bytes of the state. A chosen-plaintext attacker could then decrypt any ciphertext after storing 16 lookup tables of 256 bytes each that hold the encrypted values of each possible value of a byte.**

# AES in Python 3

```
from Crypto.Cipher import
AES
key = b"0000111122223333"
cipher = AES.new(key,
AES.MODE_ECB)
a = b"Hello from AES!!"
ciphertext =
cipher.encrypt(a)
print(ciphertext.hex())

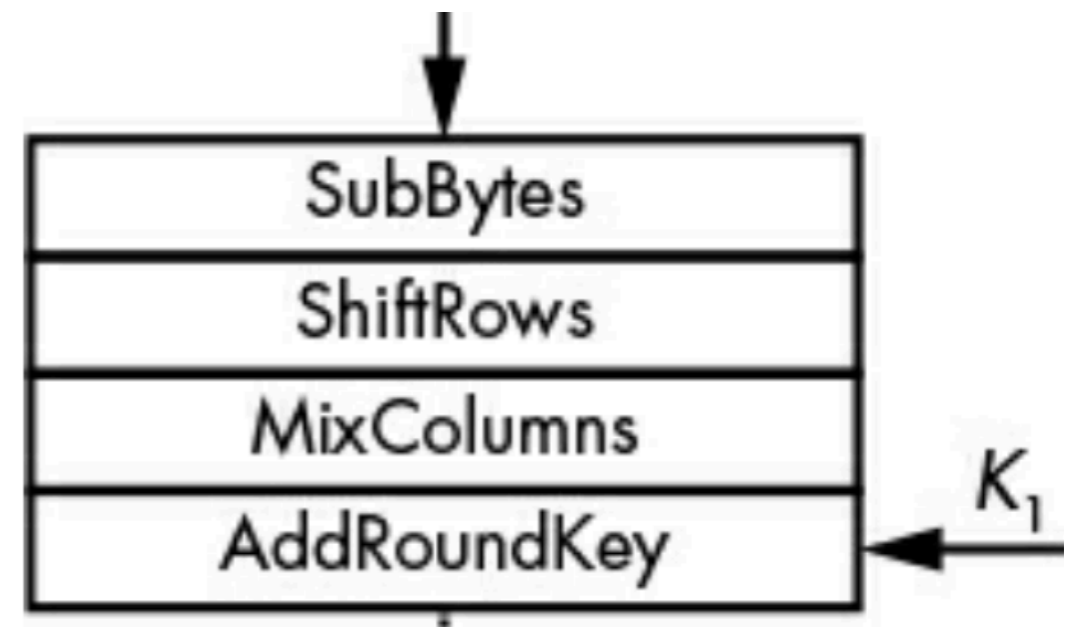
cipher = AES.new(key,
AES.MODE_ECB)
d =
cipher.decrypt(ciphertext)
print(d)
```

```
>>> from Crypto.Cipher import AES
>>> key = b"0000111122223333"
>>> cipher = AES.new(key, AES.MODE_ECB)
>>> a = b"Hello from AES!!"
>>> ciphertext = cipher.encrypt(a)
>>> print(ciphertext.hex())
59305bbea4c731a031f1423bb7cf643e
[>>>
>>> cipher = AES.new(key, AES.MODE_ECB)
>>> d = cipher.decrypt(ciphertext)
>>> print(d)
b'Hello from AES!!'
```

# Implementing AES

# Improving Efficiency

- Implementing each step as a separate function works, but it's slow
- Combining them with "table-based implementations" and "native instructions" is faster
- Using XORs and table lookups



# OpenSSL Code is Table-Based

---

```
/* round 1: */
t0 = Te0[s0 >> 24] ^ Te1[(s1 >> 16) & 0xff] ^ Te2[(s2 >> 8) & 0xff] ^ Te3[s3 & 0xff] ^ rk[ 4];
t1 = Te0[s1 >> 24] ^ Te1[(s2 >> 16) & 0xff] ^ Te2[(s3 >> 8) & 0xff] ^ Te3[s0 & 0xff] ^ rk[ 5];
t2 = Te0[s2 >> 24] ^ Te1[(s3 >> 16) & 0xff] ^ Te2[(s0 >> 8) & 0xff] ^ Te3[s1 & 0xff] ^ rk[ 6];
t3 = Te0[s3 >> 24] ^ Te1[(s0 >> 16) & 0xff] ^ Te2[(s1 >> 8) & 0xff] ^ Te3[s2 & 0xff] ^ rk[ 7];
/* round 2: */
s0 = Te0[t0 >> 24] ^ Te1[(t1 >> 16) & 0xff] ^ Te2[(t2 >> 8) & 0xff] ^ Te3[t3 & 0xff] ^ rk[ 8];
s1 = Te0[t1 >> 24] ^ Te1[(t2 >> 16) & 0xff] ^ Te2[(t3 >> 8) & 0xff] ^ Te3[t0 & 0xff] ^ rk[ 9];
s2 = Te0[t2 >> 24] ^ Te1[(t3 >> 16) & 0xff] ^ Te2[(t0 >> 8) & 0xff] ^ Te3[t1 & 0xff] ^ rk[10];
s3 = Te0[t3 >> 24] ^ Te1[(t0 >> 16) & 0xff] ^ Te2[(t1 >> 8) & 0xff] ^ Te3[t2 & 0xff] ^ rk[11];
--snip--
```

---

*Listing 4-2: The table-based C implementation of AES in OpenSSL*

# Timing Attacks

- The time required for encryption depends on the key
- Measuring timing leaks information about the key
- This is a problem with any efficient coding
- You could use slow code that wastes time
- A better solution relies on **hardware**

# Native Instructions

- **AES-NI**
  - Processor provides dedicated assembly instructions that perform AES
  - Plaintext in register **xmm0**
  - Round keys in **xmm5** to **xmm15**
- **NI** makes AES ten times faster

PXOR	%xmm5,	%xmm0
AESENC	%xmm6,	%xmm0
AESENC	%xmm7,	%xmm0
AESENC	%xmm8,	%xmm0
AESENC	%xmm9,	%xmm0
AESENC	%xmm10,	%xmm0
AESENC	%xmm11,	%xmm0
AESENC	%xmm12,	%xmm0
AESENC	%xmm13,	%xmm0
AESENC	%xmm14,	%xmm0
AESENCLAST	%xmm15,	%xmm0

# Is AES Secure?

- AES implements many good design principles
- Proven to resist many classes of cryptanalytic attacks
- But no one can foresee all possible future attacks
- So far, no significant weakness in AES-128 has been found



# Modes of Operation

# Electronic Code Book (ECB)

- Each plaintext block is encrypted the same way
- Identical plaintext blocks produce identical ciphertext blocks

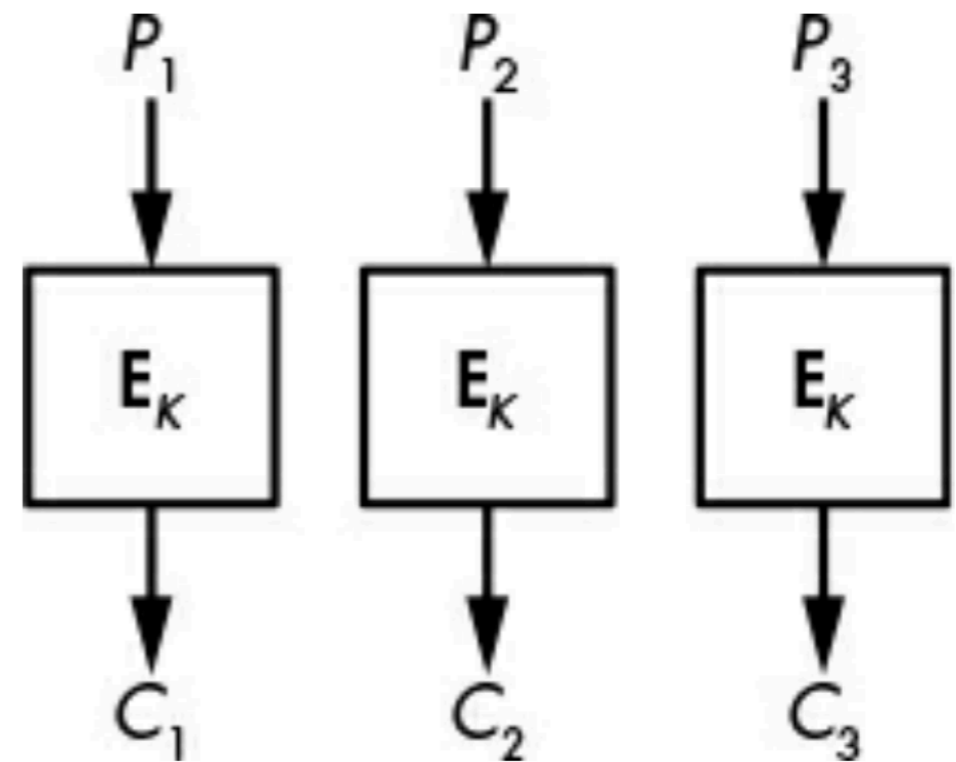


Figure 4-6: The ECB mode

# AES-ECB

- If plaintext repeats, so does ciphertext

```
plaintext = b"DEAD MEN TELL NODEAD MEN TELL NO"  
ciphertext = cipher.encrypt(plaintext)  
ciphertext.hex()
```

```
>>> plaintext = b"DEAD MEN TELL NODEAD MEN TELL NO"  
>>> ciphertext = cipher.encrypt(plaintext)  
>>> ciphertext.hex()  
'66cc2a4741a704c7849450129bd29ce566cc2a4741a704c7849450129bd29ce5'
```



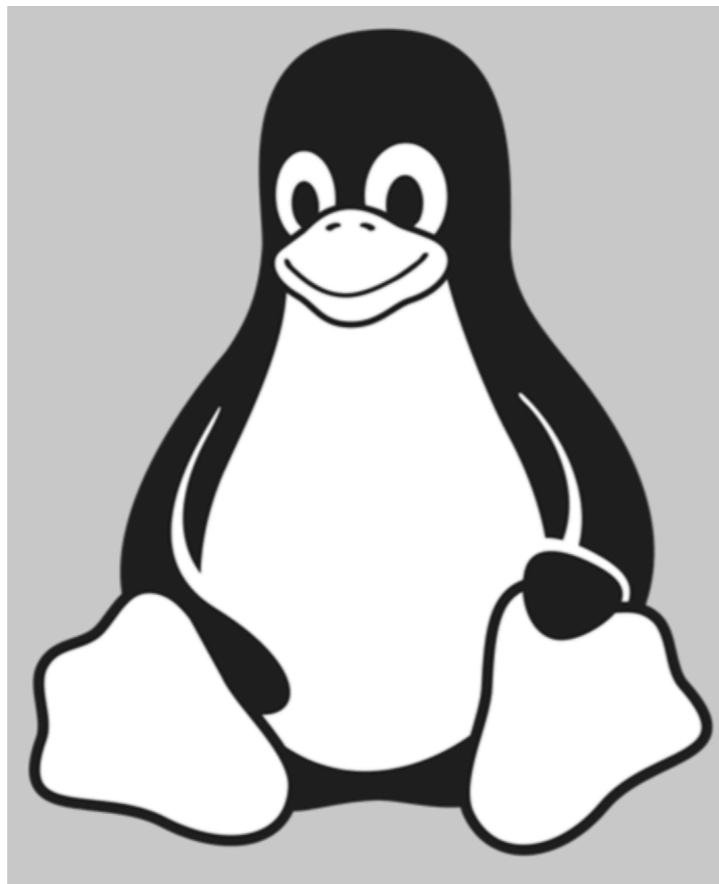
# Encrypted Password Repeats

```
./shared_prefs/com.staples.mobile.cfa.xml: <string name="encryptedPassword">  
Ex+zjrCIlgw/kkZ0dIRfPhMfs46wiJYMP5JGdHSEXz4VWo8KfvDtbU+NuhSpui58</string>
```

```
>>> a="Ex+zjrCIlgw/kkZ0dIRfPhMfs46wiJYMP5JGdHSE  
Xz4VWo8KfvDtbU+NuhSpui58"  
>>> a1 = base64.b64decode(a)  
>>> for c in a1:  
...     d = hex(ord(c))  
...     print d[2:],  
...  
13 1f b3 8e b0 88 96 c 3f 92 46 74 74 84 5f 3e  
13 1f b3 8e b0 88 96 c 3f 92 46 74 74 84 5f 3e  
15 5a 8f a 7e f0 ed 6d 4f 8d ba 14 a9 ba 2e 7c  
>>>
```

# ECB Mode

- Encrypted image retains large blocks of solid color



# Cipher Block Chaining (CBC)

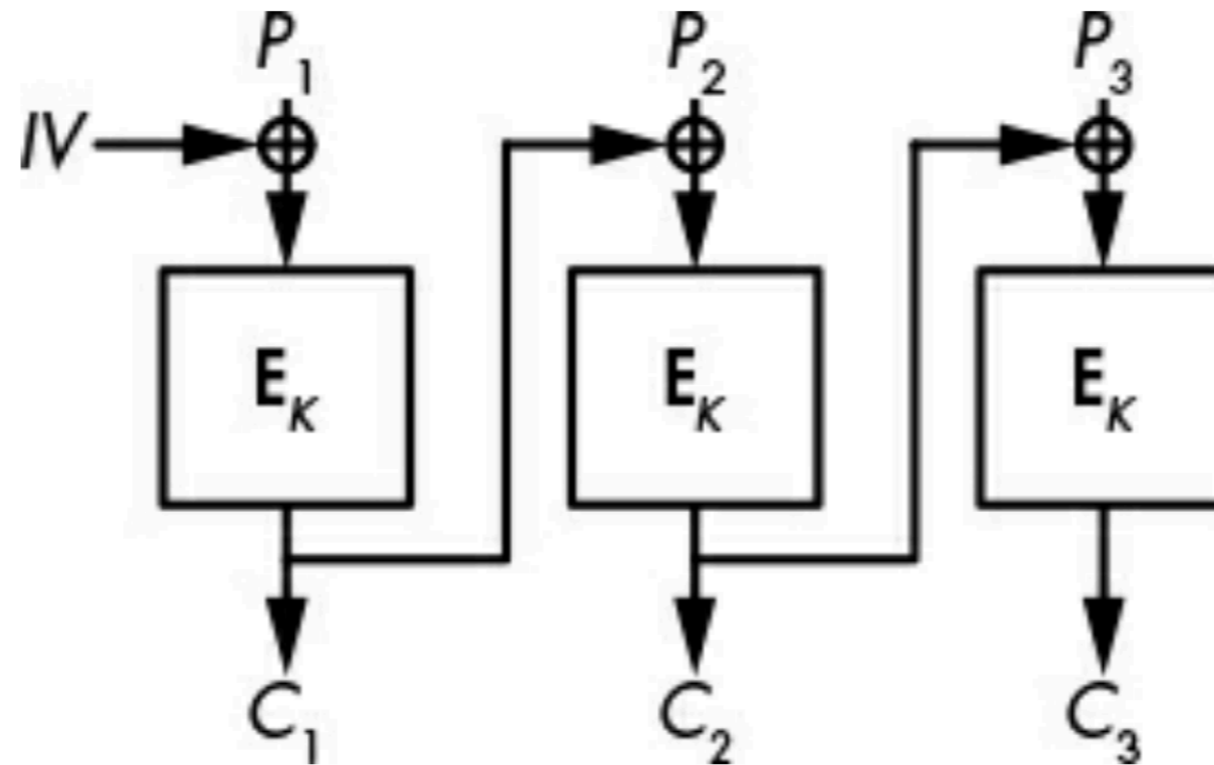
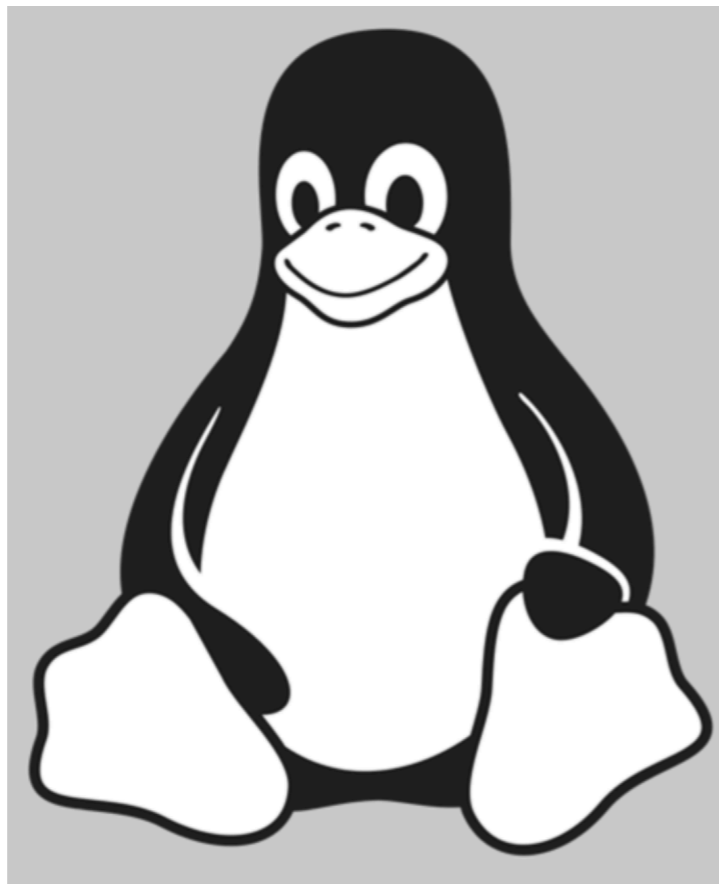


Figure 4-8: The CBC mode

- Uses a key and an **initialization vector (IV)**
- Output of one block is the **IV** for the next block
- **IV** is not secret; sent in the clear

# CBC Mode

- Encrypted image shows no patterns





# Choosing IV

- If the same IV is used every time
  - The first block is always encrypted the same way
  - Messages with the same first plaintext block will have identical first ciphertext blocks

# Parallelism

- ECB can be computed in parallel
  - Each block is independent
- CBC requires serial processing
  - Output of each block used to encrypt the next block

# Message Length

- AES requires 16-byte blocks of plaintext
- Messages must be **padded** to make them long enough

```
>>> plaintext = "HELLO"
>>> ciphertext = cipher.encrypt(plaintext)
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
  File "/usr/local/lib/python2.7/site-packages/Crypto/Cipher/blocka
lgo.py", line 244, in encrypt
    return self._cipher.encrypt(plaintext)
ValueError: Input strings must be a multiple of 16 in length
>>>
```

# PKCS#7 Padding

- If one byte of padding is needed, use **01**
- If two bytes of padding are needed, use **0202**
- If three bytes of padding are needed, use **030303**
- ...
- If fifteen bytes of padding are needed, use **0f0f0f0f0f0f0f0f0f0f0f0f**
- If no bytes of padding are needed, add an entire block of sixteen chr(16) characters, or **10101010101010101010101010101010**

- The last byte of the plaintext is always between '\x00' and '\10'
- Discard that many bytes to get original plaintext

# Padding Oracle Attack

- Almost everything uses PKCS#7 padding
- But if the system displays a "Padding Error" message the whole system shatters like glass
- That message is sufficient side-channel information to allow an attacker to forge messages without the key

# Ciphertext Stealing

- An alternative to padding
  - Prevents padding oracle attacks
- Pad with zeroes
- Swap last two blocks of ciphertext
- Discard extra bytes at the end
  - Images on next slides from Wikipedia

# Ciphertext Stealing

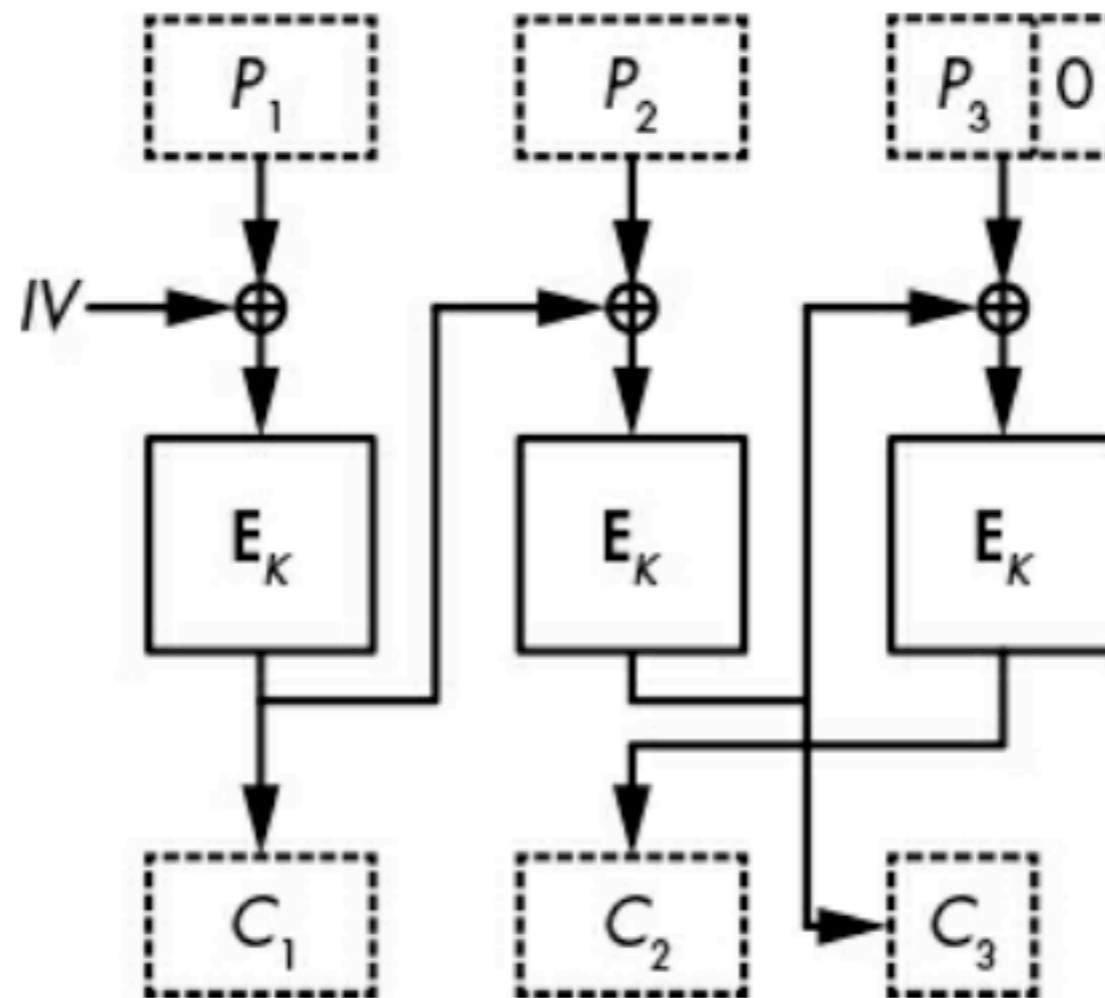


Figure 4-9: Ciphertext stealing for CBC-mode encryption

# Security of Ciphertext Stealing

- No major problems
- Inelegant and difficult to get right
- NIST SP 800-38A specifies three different ways to implement it
- Rarely used



# Counter (CTR) Mode

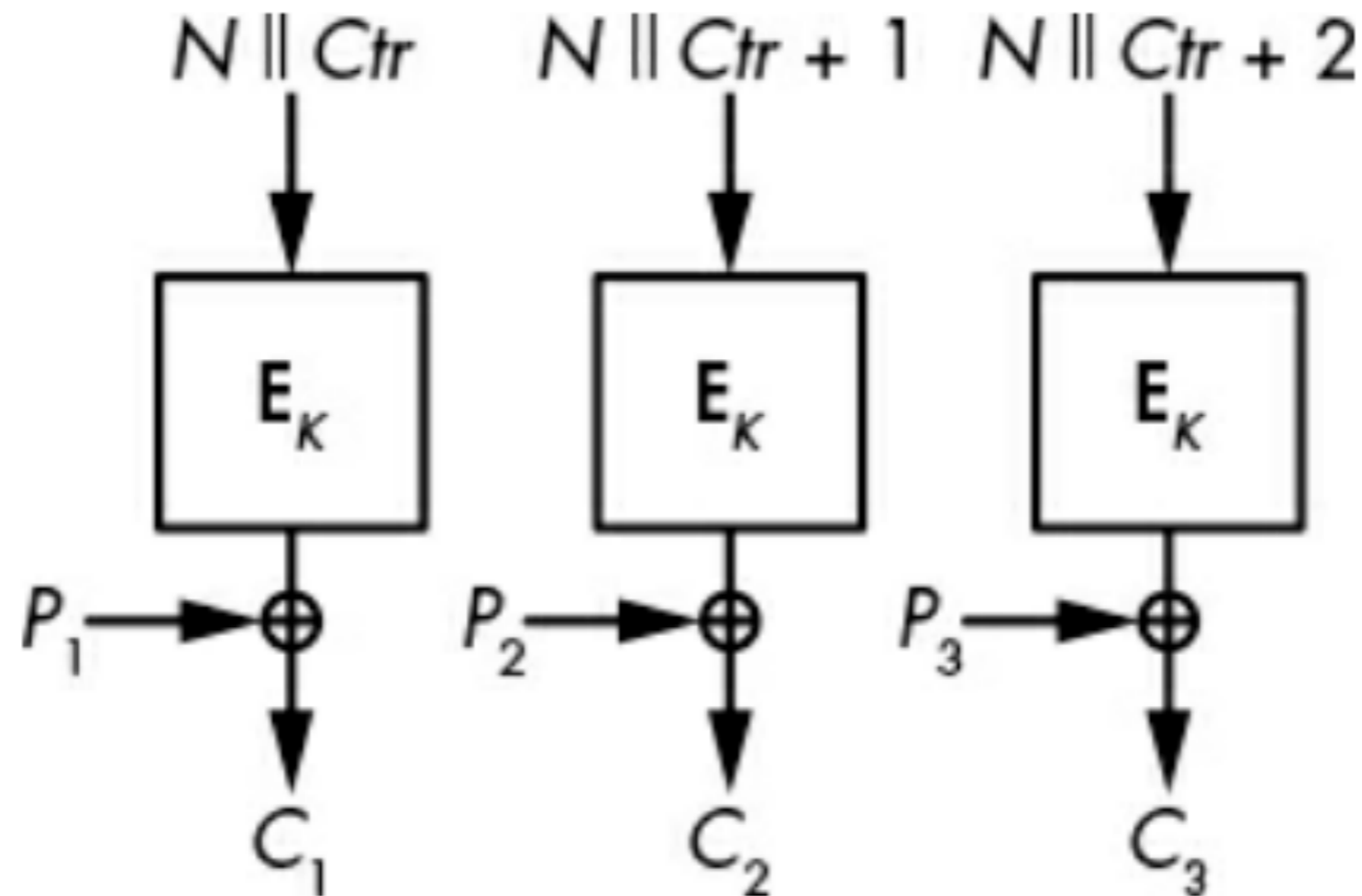


Figure 4-10: The CTR mode

- Produces a pseudorandom byte stream
- XOR with plaintext to encrypt

# Nonce

- Use a different **N** for each message
- **N** is not secret, sent in the clear

# Nonce Must not be Reused

```
$ ./aes_ctr.py
```

```
k = 130a1aa77fa58335272156421cb2a3ea
```

```
enc(00010203) = b23d284e
```

```
enc(b23d284e) = 00010203
```

- The first block produces the same bitstream if a nonce and key are re-used

# No Padding

- CTR mode uses a block cipher to produce a pseudorandom byte stream
- Creates a stream cipher
- Message can have any length
- No padding required

# Parallelizing

- CTR is faster than any other mode
- Stream can be computed in advance, and in parallel
- Before even knowing the plaintext

# How Things Can Go Wrong

# Two Attacks

- Meet-in-the-middle
- Padding oracle

# Meet-in-the-Middle Attacks

- 3DES does three rounds of DES
- Why not 2DES?

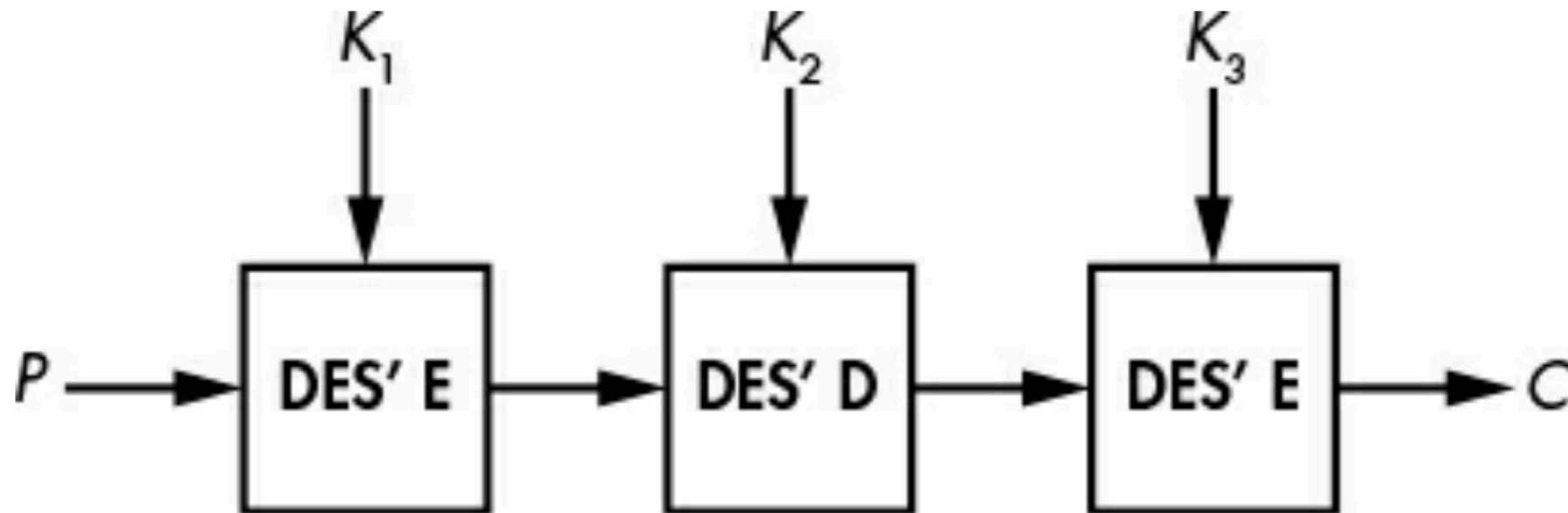


Figure 4-11: The 3DES block cipher construction



# Attacking 2DES

- Two 56-bit keys, total 112 bits
- End-to-end brute force would take  $2^{112}$  calculations

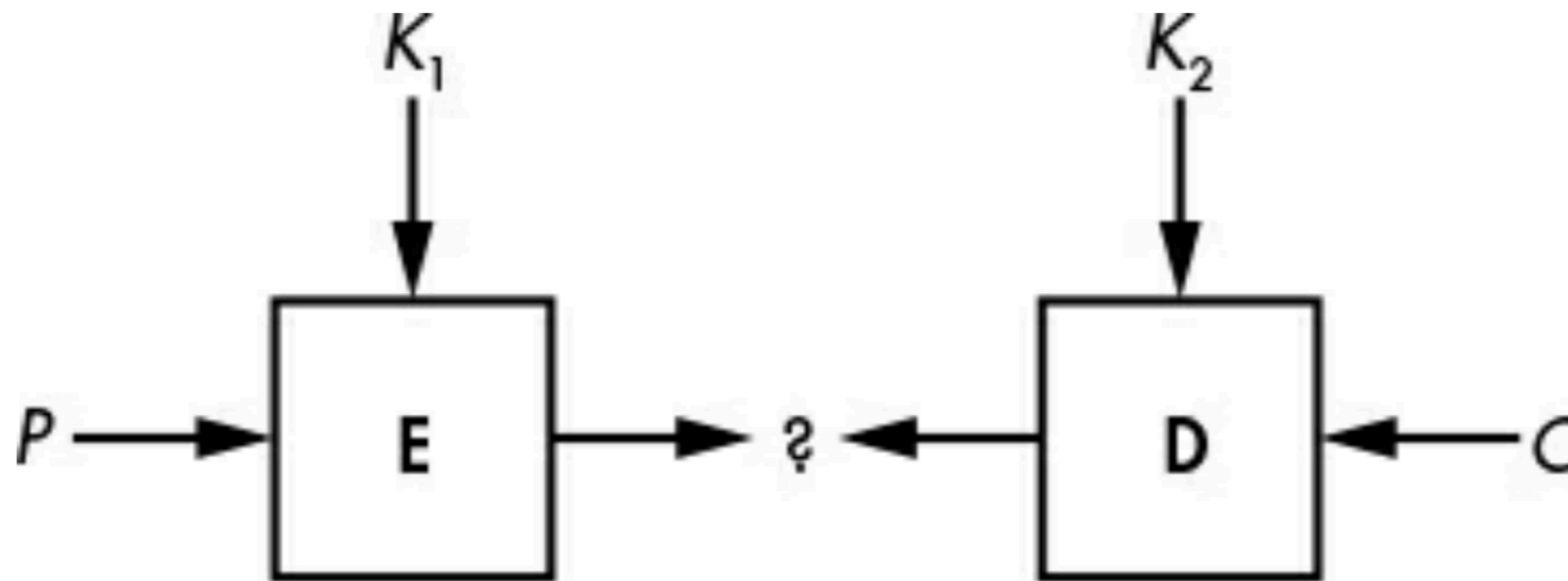


Figure 4-12: The meet-in-the-middle attack

# Attacking 2DES

- Attacker inputs known  $P$  and gets  $C$
- Wants to find  $K_1, K_2$

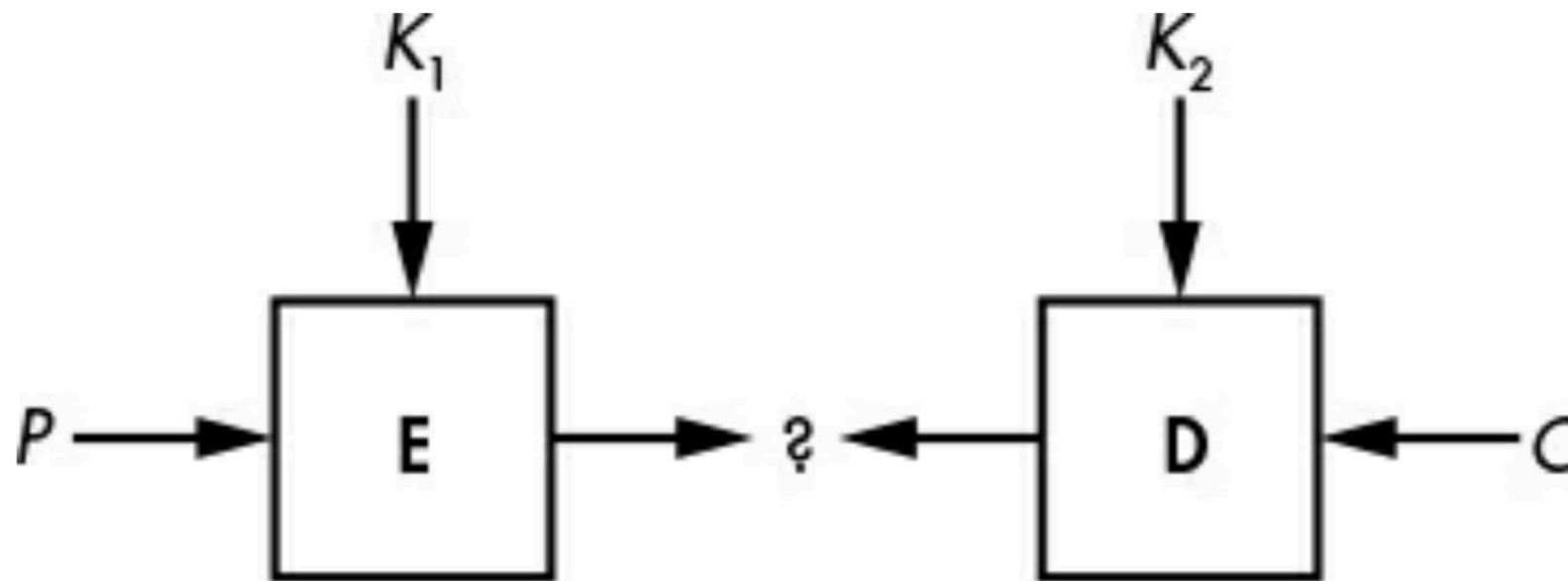


Figure 4-12: The meet-in-the-middle attack

# Attacking 2DES

- Make a list of  $E(K_1, P)$  for all  $2^{56}$  values of  $K_1$
- Make a list of  $D(K_2, P)$  for all  $2^{56}$  values of  $K_2$
- Find the item with the same values in each list
- This finds  $K_1$  and  $K_2$  with  $2^{57}$  computations

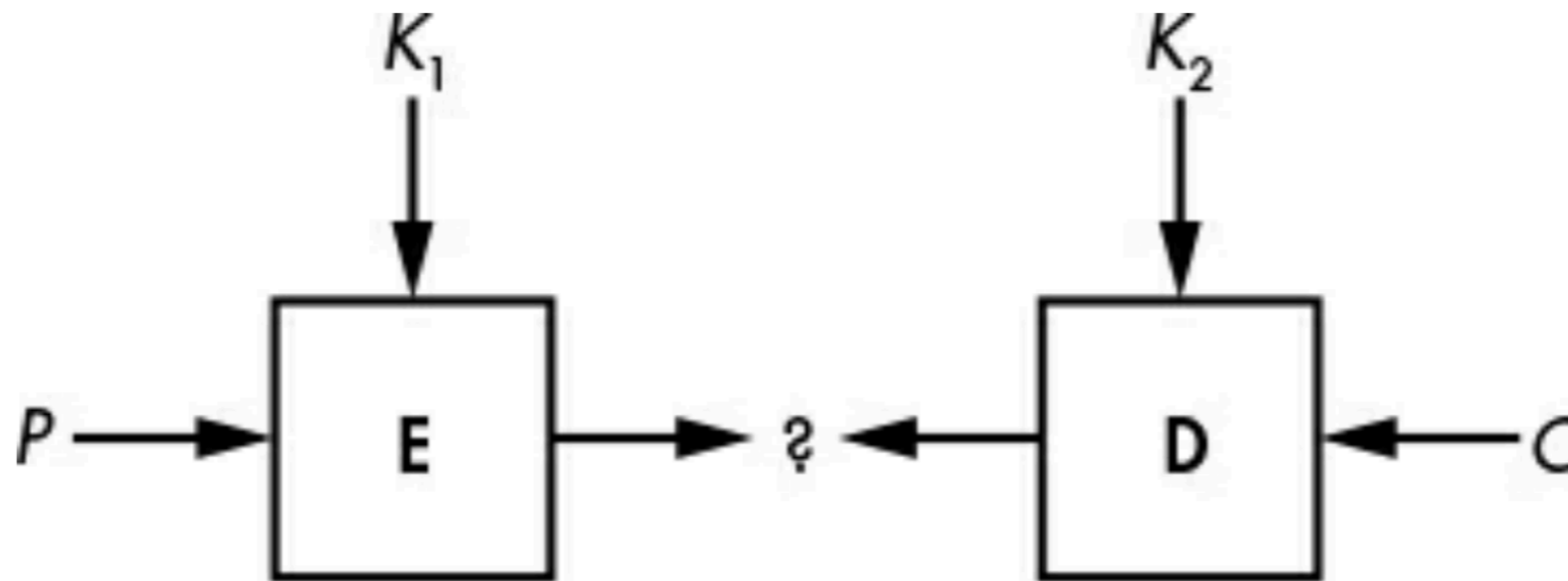


Figure 4-12: The meet-in-the-middle attack

# Meet-in-the-Middle Attack on 3DES

- One table has  $2^{56}$  entries
- The other one has  $2^{112}$  entries
- 3DES has 112 bits of security

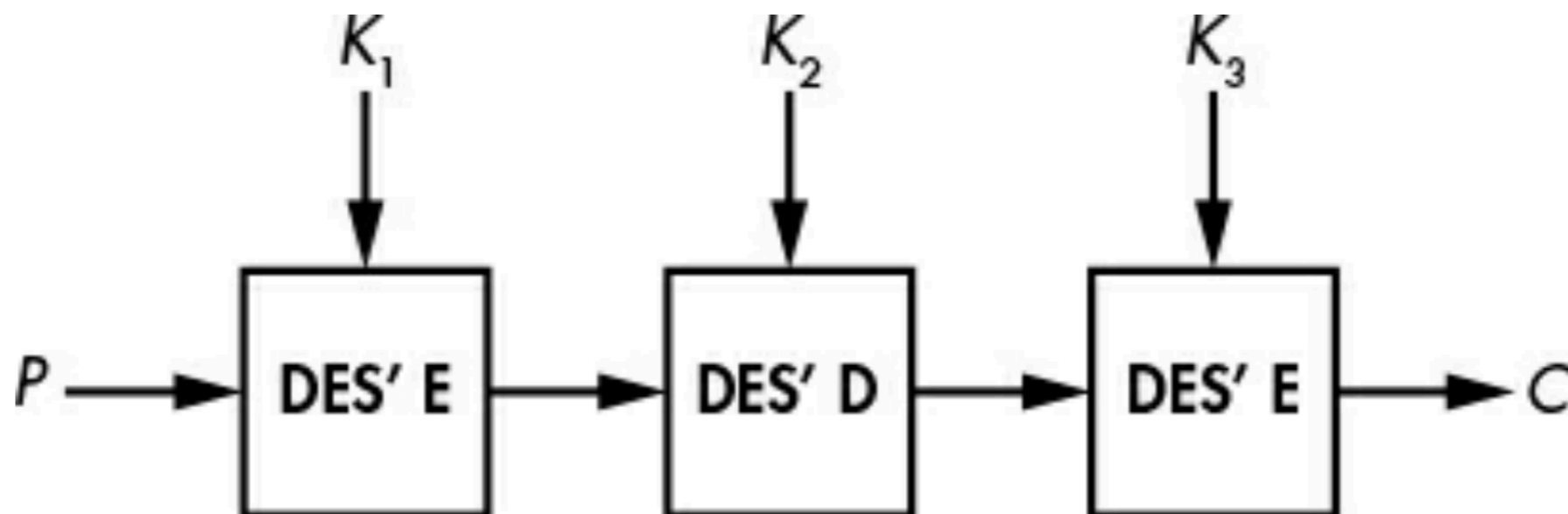
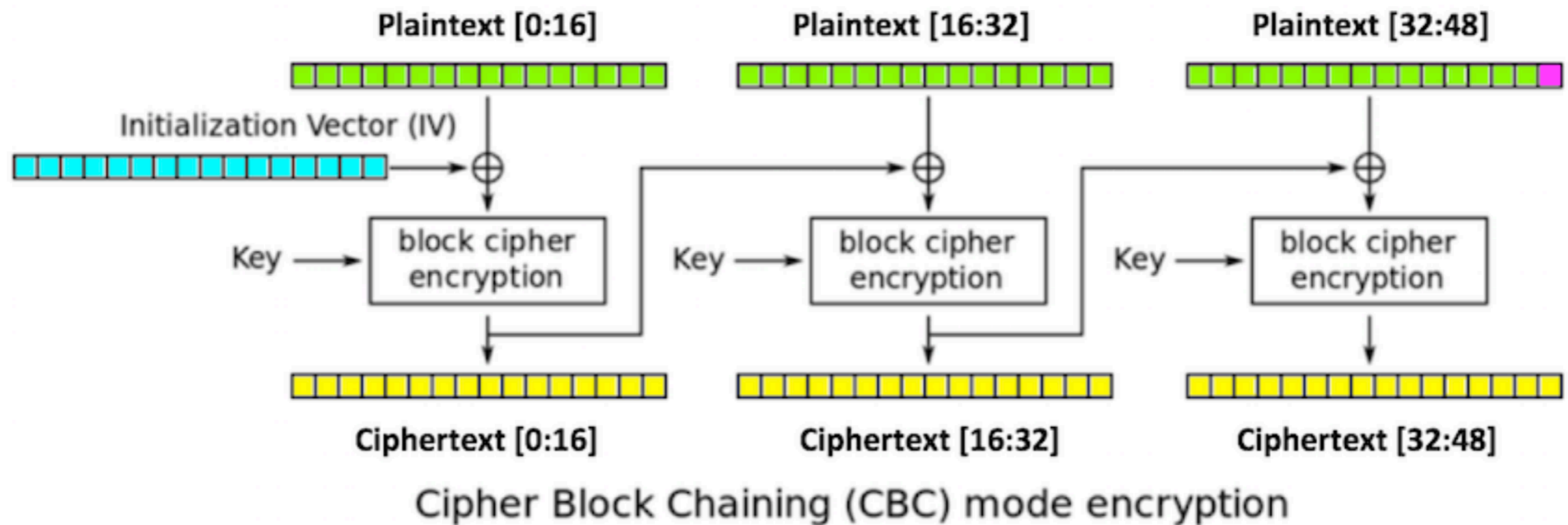


Figure 4-11: The 3DES block cipher construction

# Padding Oracle

## Encrypting 47 Bytes

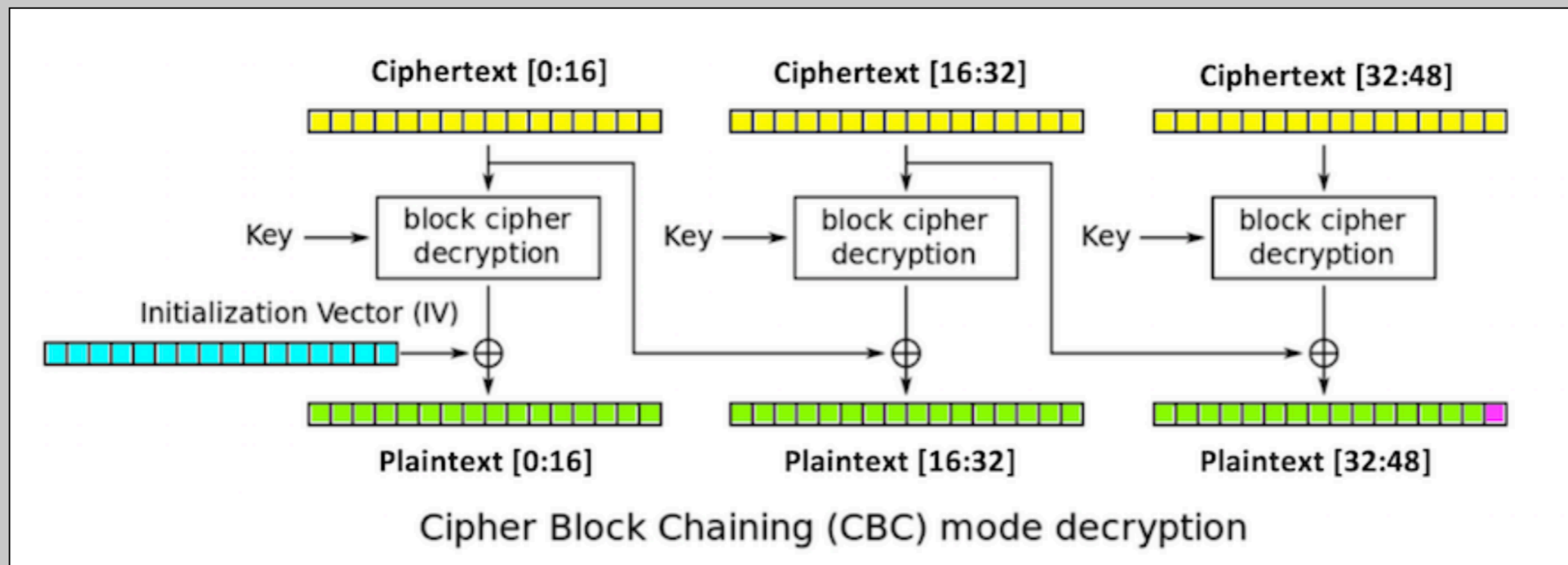
Suppose the plaintext is only 47 bytes long. In that case, a byte of **padding** (purple) must be added, as shown below.



# Padding Oracle

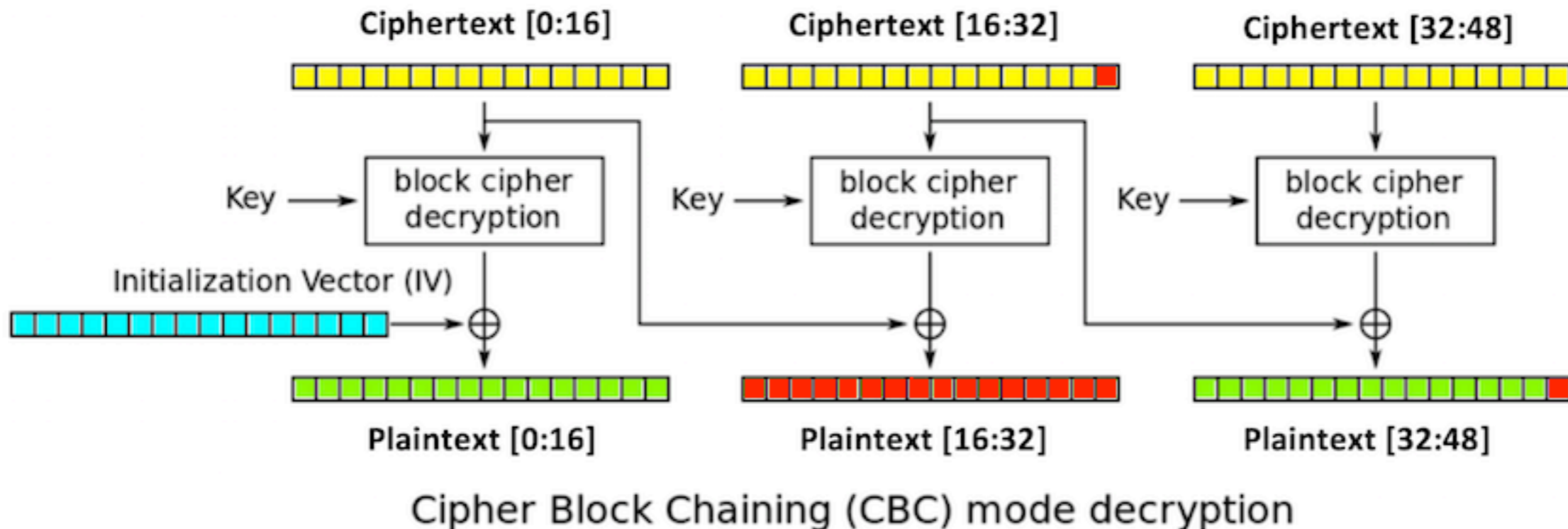
## Decryption

Using the same key and **iv** (blue), the **ciphertext** (yellow) can be decrypted to find the **plaintext** (green). The last byte is the **padding** (purple), as shown below.



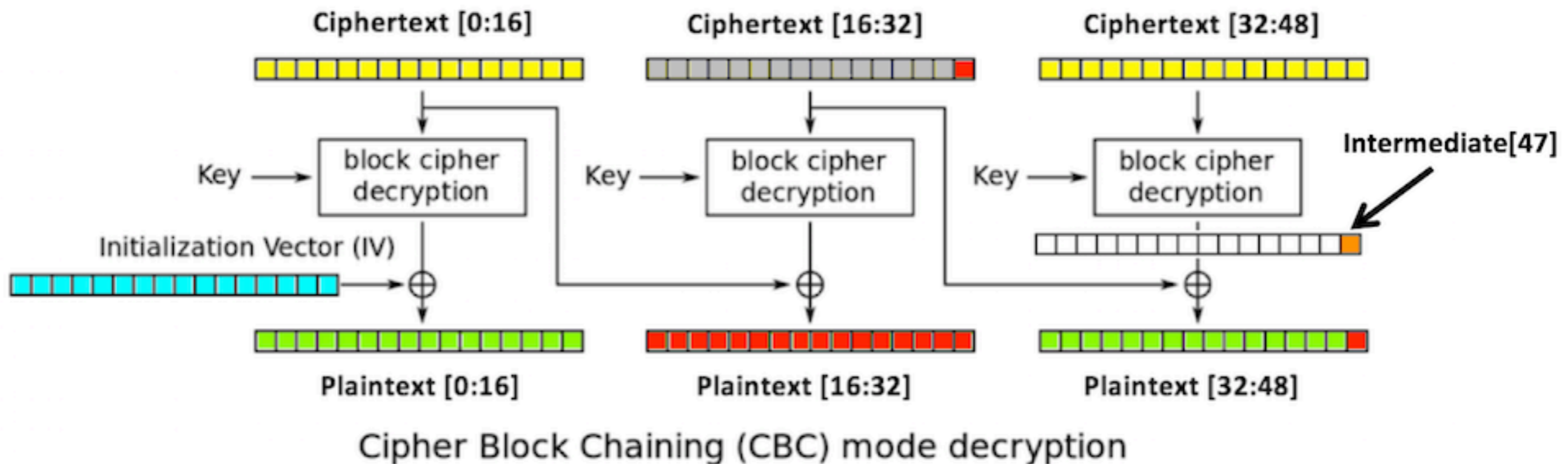
# Padding Oracle

- Change the last byte in second block
- This changes the 17 bytes shown in red



# Padding Oracle

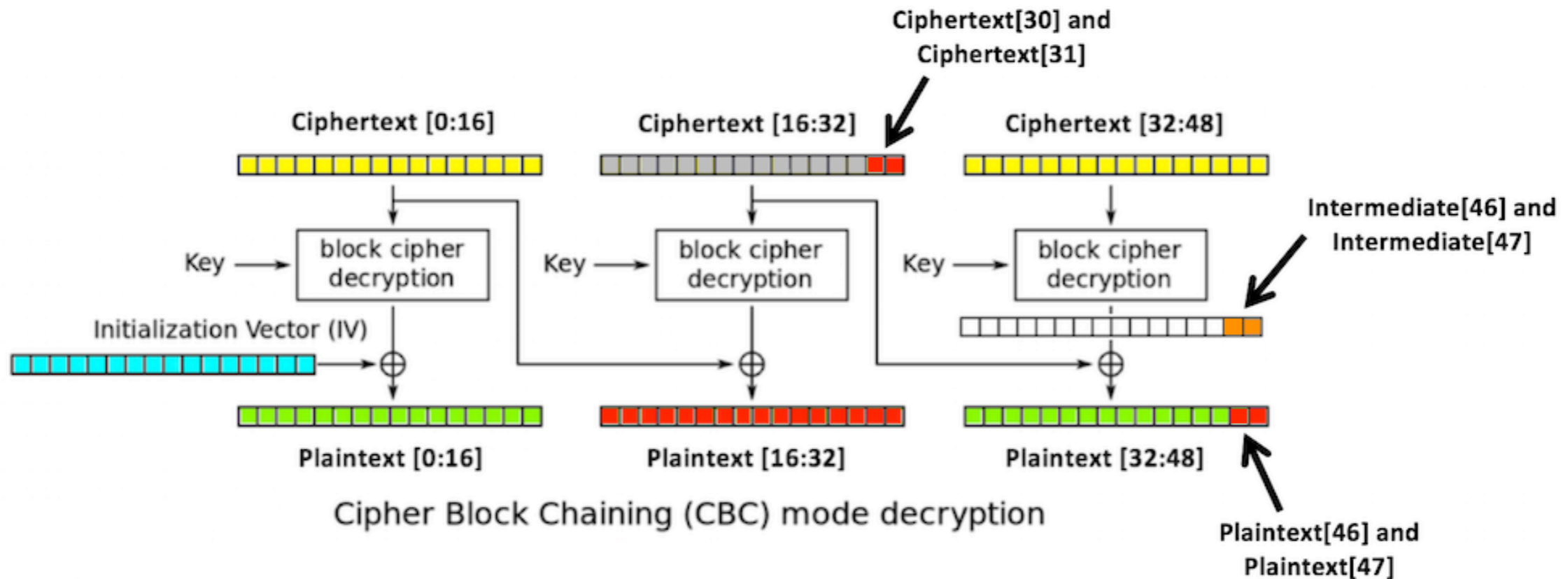
- Try all 256 values of last byte in second block
- One of them has valid padding of '\x01'
- This determines the orange byte





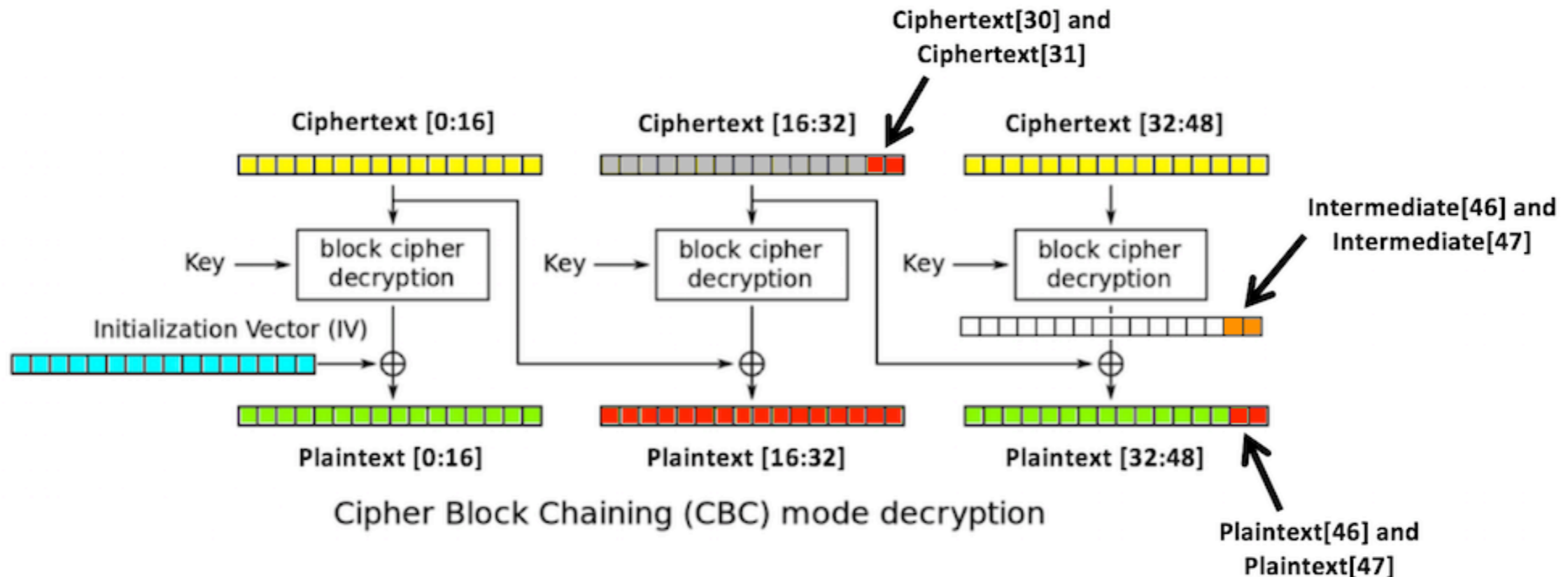
# Padding Oracle

- Continue, 256 guesses finds the next orange byte

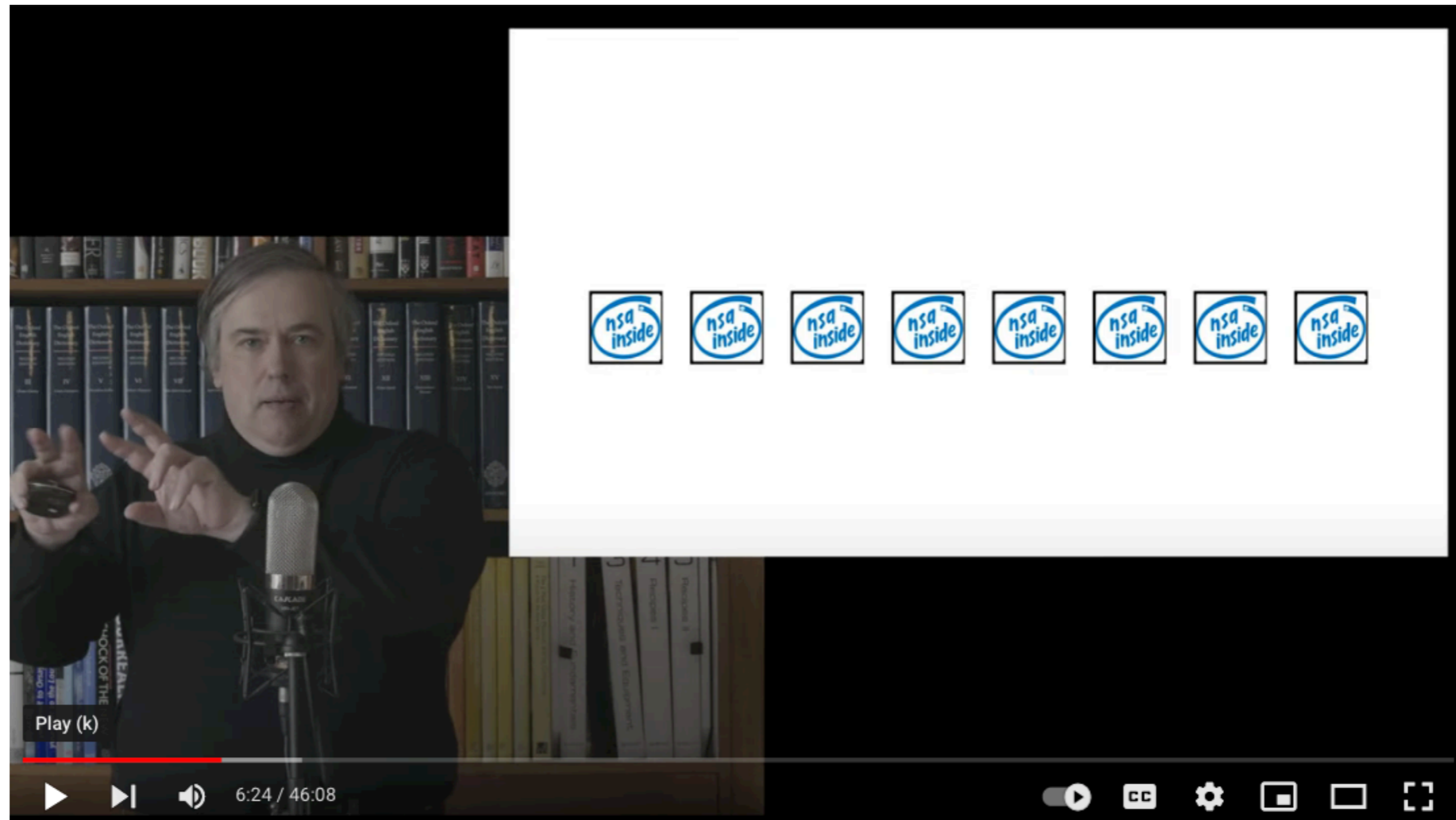


# Padding Oracle

- Once the orange bytes are known
  - Attacker can forge plaintext[32:48] to say anything



# NSA



- 3:13 - 8:40
- [https://www.youtube.com/watch?v=tPEi0mnUY\\_o](https://www.youtube.com/watch?v=tPEi0mnUY_o)

# NOBUS

- The NSA wants us to use cryptography that is
  - Weak enough so the NSA can break it
  - Strong enough so no one else can break it
- "Nobody But Us"
- This depends on the NSA keeping secrets

# Edward Snowden



- Leaked NSA secrets in 2013
- <https://www.youtube.com/watch?v=0hLjuVylIrs>

# DES and the NSA

- The NSA first weakened DES
  - Shortening the 128-bit key in the original "Lucifer" system from IBM to 56 bits
- The NSA also strengthened it
  - Improving the "S-Box" to resist differential cryptanalysis, a technique that was secret at the time
- This created a NOBUS system



4b